

A Simple Poverty Scorecard for Mali

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Abstract

This paper uses data from a national survey to construct an easy-to-use scorecard that estimates the likelihood that a household in Mali has expenditure below a given poverty line. The scorecard uses 10 simple indicators that field workers can quickly collect and verify. Poverty scores can be computed on paper in less than 5 minutes. Accuracy and sample-size formulas are reported for a range of poverty lines. Poverty scoring is a practical way for pro-poor programs in Mali to monitor poverty rates, track changes in poverty rates over time, and target services.

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Figure 1: A simple poverty scorecard for Mali

<u>Entity</u>	<u>Name</u>	<u>ID</u>	<u>Date</u> (DD/MM/YY)
Member:	_____	_____	Joined: _____
Loan officer:	_____	_____	Today: _____
Branch:			Household size: _____

<u>Indicator</u>	<u>Value</u>	<u>Points</u>	<u>Score</u>
1. How many household members are 11 years old or younger?	A. Five or more	0	
	B. Four	10	
	C. Three	13	
	D. Two	15	
	E. One	17	
	F. None	25	
2. How many members of the household usually work as their main occupation in agriculture, animal husbandry, fishing, or forestry?	A. Three or more	0	
	B. Two	7	
	C. One or none	14	
3. What is the main construction material of the roof of the residence?	A. Tile or thatch	0	
	B. Mud, corrugated metal sheets, concrete, or other	12	
4. What is the main construction material of the walls of the residence?	A. Partly cement, or other	0	
	B. Cement	7	
5. What is the household's main source of drinking water?	A. Surface water, non-modern well, drilled well, or other	0	
	B. Modern well	3	
	C. Public pump	6	
	D. Faucet tap	11	
6. What toilet arrangement does the household have?	A. Other	0	
	B. Latrine (private or shared with other households) or flush toilet (private inside, private outside, or shared with other households)	7	
7. Does the household own any television sets?	A. No	0	
	B. Yes	6	
8. Does the household own any radios?	A. No	0	
	B. Yes	7	
9. Does the household own any irons?	A. No	0	
	B. Yes	5	
10. Does the household own any motorbikes?	A. No	0	
	B. Yes	6	

Microfinance Risk Management, L.L.C., http://www.microfinance.com	Total score:
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Figure 1: A simple poverty scorecard for Mali (no points)

<u>Entity</u>	<u>Name</u>	<u>ID</u>	<u>Date</u> (DD/MM/YY)
Member:	_____	_____	Joined: _____
Loan officer:	_____	_____	Today: _____
Branch:			Household size: _____

Indicator	Value
1. How many household members are 11 years old or younger?	A. Five or more B. Four C. Three D. Two E. One F. None
2. How many members of the household usually work as their main occupation in agriculture, animal husbandry, fishing, or forestry?	A. Three or more B. Two C. One or none
3. What is the main construction material of the roof of the residence?	A. Tile or thatch B. Mud, corrugated metal sheets, concrete, or other
4. What is the main construction material of the walls of the residence?	A. Partly cement, or other B. Cement
5. What is the household's main source of drinking water?	A. Surface water, non-modern well, drilled well, or other B. Modern well C. Public pump D. Faucet tap
6. What toilet arrangement does the household have?	A. Other B. Latrine (private or shared with other households) or flush toilet (private inside, private outside, or shared with other households)
7. Does the household own any television sets?	A. No B. Yes
8. Does the household own any radios?	A. No B. Yes
9. Does the household own any irons?	A. No B. Yes
10. Does the household own any motorbikes?	A. No B. Yes

A Simple Poverty Scorecard for Mali

1. Introduction

This paper presents an easy-to-use poverty scorecard that pro-poor programs in Mali can use to monitor groups' poverty rates at a point in time, track changes in groups' poverty rates between two points in time, and target services to households.

The direct approach to poverty measurement via expenditure surveys is difficult and costly, asking households about a lengthy list of consumption items (“Did you serve breakfast today? If so, for whom? What ingredients did you use? If rice was an ingredient, how much rice did you use? Did you buy the rice, grow it yourself, or trade for it? If you bought it, how many units did you buy, how much did you pay per unit, and how often do you buy it? Now then, was oats an ingredient? . . .”).

In contrast, the indirect approach via poverty scoring is simple, quick, and inexpensive. It uses 10 verifiable indicators (such as “What is the main construction material of the floor of the residence?” or “Does the household own any television sets?”) to get a score that is highly correlated with poverty status as measured by the exhaustive expenditure survey.

The poverty scorecard here differs from “proxy means tests” (Coady, Grosh, and Hoddinott, 2002) in that it is tailored to the capabilities and purposes not of national governments but rather of local, pro-poor organizations. The feasible poverty-measurement options for these organizations are typically subjective and relative (such

as participatory wealth ranking by skilled field workers) or blunt (such as rules based on land-ownership or housing quality). Results from these approaches are not comparable across organizations nor across countries, they may be costly, and their accuracy is unknown.

If an organization wants to know what share of its participants are below a given poverty line (say, \$1/day for the Millenium Development Goals, or the poorest half below the national poverty line as required of USAID microenterprise partners), or if it wants to measure movement across a poverty line (for example, to report to the Microcredit Summit Campaign), then it needs an expenditure-based, objective tool with known accuracy. While expenditure surveys are costly even for governments, even small, local organizations can implement an inexpensive scorecard that can serve for monitoring, management, and targeting.

The statistical approach here aims to be understood by non-specialists. After all, if managers are to adopt poverty scoring on their own and apply it to inform their decisions, they must first trust that it works. Transparency and simplicity build trust. Getting “buy-in” matters; proxy means tests and regressions on the “determinants of poverty” have been around for three decades, but they are rarely used to inform decisions, not because they do not work, but because they are presented (when they are presented at all) as tables of regression coefficients incomprehensible to lay people (with cryptic indicator names such as “HHSIZE_2”, negative values, many decimal places, and

standard errors). Thanks to the predictive-modeling phenomenon known as the “flat max”, simple poverty scorecards can be almost as accurate as complex ones.

The technical approach here is also innovative in how it associates scores with poverty likelihoods, in the extent of its accuracy tests, and in how it derives sample-size formulas. Although these techniques are simple and/or standard, they have rarely or never been applied to proxy means tests.

The scorecard (Figure 1) is based on data from the 2001 *Enquête Malienne sur L’Evaluation de la Pauvreté* (EMEP, Mali Poverty Evaluation Survey) conducted by Mali’s *Direction Nationale de la Statistique et de l’Information* (DNSI). Indicators are selected to be:

- Inexpensive to collect, easy to answer quickly, and simple to verify
- Strongly correlated with poverty
- Liable to change over time as poverty status changes

All points in the scorecard are non-negative integers, and total scores range from 0 (most likely below a poverty line) to 100 (least likely below a poverty line). Non-specialists can collect data and tally scores on paper in the field in less than 5 minutes.

Poverty scoring can be used to estimate three basic quantities. First, it can estimate a household’s “poverty likelihood”, that is, the probability that the household has per-capita expenditure below a given poverty line.

Second, poverty scoring can estimate the poverty rate of a group of households at a point in time. This is simply the average poverty likelihood among the households in the group.

Third, poverty scoring can estimate changes in the poverty rate for a group of households between two points in time. This estimate is simply the change in the average poverty likelihood of the households in the group over time.

Poverty scoring can also be used for targeting. To help managers choose a targeting cut-off, this paper reports the share of Mali's households who are below a given poverty line and who are also at or below a given score cut-off.

This paper presents a single scorecard (Figure 1) whose indicators and points were derived using the national poverty line and a sub-sample of Mali's EMEP. Scores from this scorecard are calibrated to poverty likelihoods for six poverty lines.

Scorecard accuracy is tested on a different sub-sample of the EMEP than that used in scorecard construction. While all three scoring estimators are unbiased (that is, they match the true value on average in repeated samples from the 2001 population), they are—like all predictive models—biased to some extent when applied to a different population.

Thus, while the indirect scoring approach is less costly than the direct survey approach, it is also biased. (The survey approach is unbiased by assumption.) There is bias because scoring must assume that the future relationship between indicators and poverty will be the same as in the data used to build the scorecard. Of course, this assumption—ubiquitous and inevitable in predictive modelling—holds only partly.

The difference between scorecard estimates of groups' poverty rates and the true rates ranges from -0.7 percentage points for the \$2/day line to 5.0 percentage points for

the \$3/day line, with an average absolute difference across all six lines of 2.7 percentage points. These differences are due to sampling variation—not bias—because their average would be zero if the EMEP were to be repeatedly redrawn and divided into sub-samples before repeating the entire scorecard-building process.

For sample sizes of $n = 16,384$, the 90-percent confidence intervals for these estimated differences are less than ± 1.0 percentage points. For $n = 1,024$, the 90-percent intervals are less than ± 4.0 percentage points.

Section 2 below describes data and poverty lines. Section 3 compares the new scorecard to an existing poverty scorecard for Mali. Sections 4 and 5 describe scorecard construction and offer practical guidelines for use. Sections 6 and 7 detail the estimation of households' poverty likelihoods and of groups' poverty rates at a point in time. Section 8 discusses estimating changes in poverty rates between two points in time. Section 9 covers targeting. The final section is a summary.

2. Data and poverty lines

This section discusses the data used to construct and test the poverty scorecard. It also presents the poverty lines to which scores are calibrated.

The scorecard is based on Mali’s 2001 EMEP. DNSI (2004) reports that the EMEP covers 7,373 households, but the database provided by the DNSI for this paper includes only 4,933 households. Still, the sum of household weights (themselves weighted by household size) match Mali’s 10.2 million population in DNSI (2004). Thus, the missing households appear to have been removed deliberately (albeit without documentation), with remaining households reweighted to maintain representativeness.

Here, EMEP households are randomly divided into three samples (Figure 2):¹

- *Construction* for selecting indicators and points
- *Calibration* for associating scores with poverty likelihoods
- *Validation* for testing accuracy on data not used in construction or calibration

Mali has two official poverty lines (DNSI, 2004). The food line is based on the expenditure—derived from the 2001 EMEP—required to obtain 2,450 calories

¹ The average household in the EMEP represents about 220 households. Before random assignment to sub-samples, households representing more than 500 households are replicated—and their weights evenly divided among their replicates—so that each replicate represents less than 500 households. Of course, the newly replicated households together represent the same number of households as the original heavily weighted household. This replication helps spread heavily weighted households across the construction, calibration, and validation sub-samples, which in turn reduces the influence of any single heavily weighted household on scorecard construction or testing. This does not affect the unbiasedness of scoring estimators in repeated samples, but it does increase precision and thus decreases the average difference between estimates and true values in any given sample (such as the validation sample). It also helps prevent bootstrap estimates from breaking down (see Singh, 1998).

(Fcfa271/person/day). The national line is the actual total expenditure (on food and non-food) by people in the EMEP who consume about 2,450 calories per day (Fcfa395/person/day).

The national line and the food line are not adjusted for household economies of scale nor for differences in cost-of-living by urban/rural or region (DNSI, 2004). Indeed, there are no sub-national price indices for Mali.

Because local pro-poor organizations may want to use different poverty lines, this paper calibrates scores from its single scorecard (constructed using the national line) to poverty likelihoods for six lines (figures in parentheses are per-capita daily poverty lines and household-level poverty rates from Figure 2):

- National line (Fcfa395, 57.3 percent)
- Food line (Fcfa271, 38.0 percent)
- USAID “extreme” line (Fcfa228, 28.6 percent)
- \$1/day (Fcfa215, 25.4 percent)
- \$2/day (Fcfa431, 61.7 percent)
- \$3/day (Fcfa646, 80.1 percent)

The USAID “extreme” line (U.S. Congress, 2002) is the median expenditure of households below the national line.

The \$1/day line is derived from the following data:

- 1993 purchase-power parity exchange rate: Fcfa124.89 per \$1
- 1993 CPI (average): 65.87
- 2001 CPI (average): 105.19

The \$1/day line is then $124.89 \times (105.19 / 65.87) \times 1.08 = \text{Fcfa}215.40$ (Sillers, 2006). The \$2/day and \$3/day lines are multiples of the \$1/day line.

Poverty rates may be at the person-level or the household-level. The person-level rate is the share of people in a given group who live in households whose per-capita expenditure (that is, total household expenditure divided by the number of household members) is below a given poverty line. The person-level rates in Figure 2 for the national line and the food line match those in DNSI (2004).

The household-level poverty rate is the share of households in a given group whose per-capita expenditure is below a given poverty line.

Whereas governments report person-level poverty rates, local pro-poor development organizations typically report household-level poverty rates. This is because local organizations want to know the poverty rate of their clients, not the poverty rate of all people who live in households with their clients.

Given household-level poverty likelihoods, the person-level poverty rate for all people in a group of households is simply the average of the household-level poverty likelihoods, weighted by the number of people in each household. Larger households are more likely to be poor, so the person-level rate exceeds the household-level rate.

3. An existing poverty scorecard for Mali

Morris *et al.* (1999) use 1997 data on 275 households in Mali's rural Lacustrine region to test an approach to poverty scoring that measures "socioeconomic position" inexpensively so that it can be included in health surveys and epidemiological studies.

Their indicators are 18 agricultural implements owned by men, 16 kitchen items owned by women, and about 14 non-gendered consumer durables such as bicycles, lamps, and chairs. Each indicator's value is defined as the number of the item that the household owns. Each indicator's points are defined as the reciprocal of the share of households that own the item, so rarer items get more points. (For example, if one-third of households own gas lamps, then each gas lamp owned gets $1 \div (1 \div 3) = 3$ points.) The total score is the logarithm of the sum of each indicator multiplied by its points.

Socioeconomic status is defined as the logarithm of the total value of household assets. Morris *et al.* then measure accuracy as the correlation coefficient between the score and socioeconomic status.

The new scorecard here differs from Morris *et al.* in several ways. First, it has a directly practical purpose: to help local, pro-poor programs in Mali improve their service quality and outreach to the poor. In contrast, Morris *et al.* have purely methodological aims; indeed, they do not report their scorecard's indicators or points.

Second, the new scorecard here is based on a nationally representative database that is newer and larger.

Third, the new scorecard defines socioeconomic status as whether per-capita household expenditure is below a given poverty line. This is more commonly used in practice than the logarithm of the value of household assets.

Fourth, the new scorecard produces poverty likelihoods that have absolute units (scores from Morris *et al.* have relative units). Furthermore, poverty likelihoods can be used not only as controls in epidemiological regressions but also for targeting and for estimating groups' poverty rates and their changes over time.

Fifth, the new scorecard is tested on data that is not used in its construction. In contrast, Morris *et al.* build and test their scorecard with the same data, leading to overstated accuracy. Beyond correlation coefficients, this paper reports differences between estimates and true values, precision, and sample-size formulas.

Sixth, the new scorecard is less costly than Morris *et al.* (10 indicators versus about 40) and simpler for non-specialists to understand (no reciprocals or logarithms).

4. Scorecard construction

About 100 potential indicators are initially prepared in the areas of:

- Family composition (such as female headship and number of children)
- Education (such as school attendance by children and highest grade completed)
- Employment (such as sector and salaried status)
- Housing (such as tenancy status and type of construction)
- Ownership of durable goods (such as televisions, refrigerators, and automobiles)

Indicators are first screened with the entropy-based “uncertainty coefficient” (Goodman and Kruskal, 1979) that measures how well an indicator predicts poverty on its own. Figure 3 lists the best indicators, ranked by uncertainty coefficient. Responses are ordered starting with those most strongly associated with poverty.

Many indicators in Figure 3 are similar to each other in terms of their association with poverty. For example, few houses with dirt floors have cement walls or tile roofs. If a scorecard includes roof and walls, then data on the floor adds little information about poverty. Thus, many indicators strongly associated with poverty are not in the scorecard, as they are similar to other indicators that are included.

The scorecard also aims to measure changes in poverty through time. Thus, some powerful indicators (such as the highest grade completed by a household member) that are relatively insensitive to changes in poverty are omitted in favor of less-powerful indicators (such as ownership of radios or irons) that are more sensitive.

The scorecard itself is built using Logit regression on the construction sub-sample (Figure 2). Indicator selection uses both judgment and statistics (forward stepwise based on “c”). The first step is to build one scorecard for each candidate indicator,

using Logit to derive points. Each scorecard’s accuracy is taken as “c”, a measure of the ability to rank by poverty status (SAS Institute Inc., 2004).

One of these one-indicator scorecards is then selected based on several factors (Schreiner *et al.*, 2004; Zeller, 2004), including improvement in accuracy, likelihood of acceptance by users (determined by simplicity, cost of collection, and “face validity” in terms of experience, theory, and common sense), sensitivity to changes in poverty status, variety among indicators, and verifiability.

A series of two-indicator scorecards are then built, each based on the one-indicator scorecard selected from the first step, with a second candidate indicator added. The best two-indicator scorecard is then selected, again based on “c” and judgment. These steps are repeated until the scorecard has 10 indicators.

The final step is to transform the Logit coefficients into non-negative integers such that total scores range from 0 (most likely below a poverty line) to 100 (least likely below a poverty line).

This algorithm is the Logit analogue to the familiar R^2 -based stepwise with least-squares regression. It differs from naïve stepwise in that the criteria for selecting indicators include not only statistical accuracy but also judgment and non-statistical factors. The use of non-statistical criteria can improve robustness through time and, more important, helps ensure that indicators are simple and make sense to users.

The single poverty scorecard here applies to all of Mali. Evidence from India and Mexico (Schreiner, 2006a and 2005a), Sri Lanka (Narayan and Yoshida, 2005), and

Jamaica (Grosh and Baker, 1995) suggests that segmenting scorecards by rural/urban does not improve accuracy much.

5. Practical guidelines for scorecard use

The main challenge of scorecard design is not to squeeze out the last drops of accuracy but rather to improve the chances that scoring is actually used (Schreiner, 2005b). When scoring projects fail, the reason is not usually technical inaccuracy but rather the failure of an organization to decide to do what is needed to integrate scoring in its processes and to learn to use it properly (Schreiner, 2002). After all, most reasonable scorecards predict tolerably well, thanks to the empirical phenomenon known as the “flat max” (Hand, 2006; Baesens *et al.*, 2003; Lovie and Lovie, 1986; Kolesar and Showers, 1985; Stillwell, Hutton, and Edwards, 1983; Dawes, 1979; Wainer, 1976; Myers and Forgy, 1963). The bottleneck is less technical and more human, not statistics but organizational change management. Accuracy is easier to achieve than adoption.

The scorecard here is designed to encourage understanding and trust so that users will adopt it and use it properly. Of course, accuracy matters, but it is balanced against simplicity, ease-of-use, and “face validity”. Programs are more likely to collect data, compute scores, and pay attention to the results if, in their view, scoring does not make a lot of “extra” work and if the whole process generally seems to make sense.

To this end, the scorecard here fits on one page (Figure 1). The construction process, indicators, and points are simple and transparent. “Extra” work is minimized; non-specialists can compute scores by hand in the field because the scorecard has:

- Only 10 indicators
- Only categorical indicators
- Simple weights (non-negative integers, with no arithmetic beyond addition)

The scorecard in Figure 1 is ready to be photocopied. It can also serve as a template for data-entry screens with database software (or a simple spreadsheet, see Schreiner, 2008a) that records identifying information for the participant, dates, indicators, indicator values, scores, and poverty likelihoods.

A field worker using the paper scorecard would:

- Record participant identifiers
- Read each question from the scorecard
- Circle the response and its points
- Write the points in the far-right column
- Add up the points to get the total score
- Implement targeting policy (if any)
- Deliver the paper scorecard to a central office for filing or data entry

Of course, field workers must be trained. Quality results depend on quality inputs. If organizations or field workers gather their own data and have an incentive to exaggerate poverty rates (for example, if they are rewarded for higher poverty rates), then it is wise to do on-going quality control via data review and random audits (Matul and Kline, 2003).² IRIS Center (2007a) and Toohig (2007) are useful nuts-and-bolts guides for budgeting, training field workers and supervisors, logistics, sampling, interviewing, piloting, recording data, and quality control.

² If an organization does not want field workers to know the points associated with indicators, then they can use the version of Figure 1 without points and apply the points later in a spreadsheet or database at the central office.

In terms of sampling design, an organization must make choices about:

- Who will do the scoring
- How scores will be recorded
- What participants will be scored
- How many participants will be scored
- How frequently participants will be scored
- Whether scoring will be applied at more than one point in time
- Whether the same participants will be scored at more than one point in time

The non-specialists who apply the scorecard with participants in the field can be:

- Employees of the organization
- Third-party contractors

Responses, scores, and poverty likelihoods can be recorded:

- On paper in the field and then filed at an office
- On paper in the field and then keyed into a database or spreadsheet at an office
- In portable electronic devices in the field and then downloaded to a database

The subjects to be scored can be:

- All participants (or all new participants)
- A representative sample of all participants (or of all new participants)
- All participants (or all new participants) in a representative sample of branches
- A representative sample of all participants (or of all new participants) in a representative sample of branches

If not determined by other factors, the number of participants to be scored can be derived from sample-size formulas (presented later) for a desired level of confidence and a desired confidence interval.

Frequency of application can be:

- At in-take only (precluding measuring change in poverty rates)
- As a once-off project for current participants (precluding measuring change)
- Once a year or at some other fixed interval (allowing measuring change)
- Each time a field worker visits a participant at home (allowing measuring change)

When the scorecard is applied more than once so as to measure change in poverty rates, it can be applied:

- With two different representative samples
- With a single sample, scored twice

An example set of choices were made by BRAC and ASA, two microlenders in Bangladesh (each with 7 million participants) who are applying a poverty scorecard similar to the one here (Schreiner, 2006b). Their design is that loan officers in a random sample of branches score all participants each time they visit a homestead as part of their standard due diligence prior to loan disbursement (about once a year). Responses are recorded on paper in the field before being sent to a central office to be entered into a database. ASA's and BRAC's sampling plans cover 50,000–100,000 participants each.

6. Estimates of household poverty likelihoods

The sum of scorecard points for a household is called the *score*. For Mali, scores range from 0 (most likely below a poverty line) to 100 (least likely below a poverty line). While higher scores indicate less likelihood of being below a poverty line, the scores themselves have only relative units. For example, doubling the score does not double the likelihood of being above a poverty line.

To get absolute units, scores must be converted to *poverty likelihoods*, that is, probabilities of being below a poverty line. This is done via simple look-up tables. For the example of the national line, scores of 5–9 have a poverty likelihood of 86.9 percent, and scores of 50–54 have a poverty likelihood of 47.4 percent (Figure 4).

The poverty likelihood associated with a score varies by poverty line. For example, scores of 50–54 are associated with a poverty likelihood of 47.4 percent for the national line but 10.2 percent for the \$1/day line.³

6.1 Calibrating scores with poverty likelihoods

A given score is non-parametrically associated (“calibrated”) with a poverty likelihood by defining the poverty likelihood as the share of households in the calibration sub-sample who have the score and who are below a given poverty line.

³ Starting with Figure 4, most figures have six versions, one for each poverty line. To keep them straight, they are grouped by poverty line. Single tables that pertain to all poverty lines are placed with the tables for the national line.

For the example for the national line, there are 302 households in the calibration sub-sample with a score of 5–9, of whom 262 are below the poverty line (Figure 5). The estimated poverty likelihood associated with a score of 5–9 is then 86.9 percent, because $262 \div 302 = 86.9$ percent.

To illustrate with the national line and a score of 50–54, there are 8,033 households in the calibration sub-sample, of whom 3,807 are below the line (Figure 5). Thus, the poverty likelihood for this score is $3,807 \div 8,033 = 47.4$ percent.

The same method is used to calibrate scores with estimated poverty likelihoods for the other poverty lines.

Figure 6 shows, for all scores, the likelihood that expenditure falls in a range demarcated by two adjacent poverty lines. For example, the daily expenditure of someone with a score of 50–54 falls in the following ranges with probability:

- 10.2 percent below \$1/day
- 8.8 percent between \$1/day and the food line
- 28.4 percent between the food line and the national line
- 41.3 percent between the national line and \$3/day
- 11.3 percent above \$3/day

Even though the scorecard is constructed partly based on judgment, the calibration process produces poverty likelihoods that are objective, that is, derived from data on expenditure-based poverty lines. The poverty likelihoods are objective even if indicators and/or points are selected without any data at all. In fact, objective scorecards of proven accuracy are often based only on judgment (Fuller, 2006; Caire, 2004; Schreiner *et al.*, 2004). Of course, the scorecard here was constructed with both

data and judgement. The fact that this paper acknowledges that some choices in scorecard construction—as in any statistical analysis—are informed by judgment in no way impugns the objectivity of the poverty likelihoods, as this depends on using data in score calibration, not on using data (and nothing else) in scorecard construction.

Although the points in Mali’s poverty scorecard are transformed coefficients from a Logit regression, scores are not converted to poverty likelihoods via the Logit formula of $2.718281828^{\text{score}} \times (1 + 2.718281828^{\text{score}})^{-1}$. This is because the Logit formula is esoteric and difficult to compute by hand. It is more intuitive to define the poverty likelihood as the share of households with a given score who are below a poverty line. In the field, converting scores to poverty likelihoods requires no arithmetic at all, just a look-up table. This non-parametric calibration can also improve accuracy, especially with large calibration samples.

6.2 Accuracy of estimates of poverty likelihoods

As long as the relationship between indicators and poverty does not change, this calibration process produces unbiased estimates of poverty likelihoods. *Unbiased* means that in repeated samples from the same population, the average estimate matches the true poverty likelihood. The scorecard also produces unbiased estimates of poverty rates at a point in time and of changes in poverty rates between two points in time.⁴

⁴ This follows because these estimates of groups’ poverty rates are linear functions of the unbiased estimates of households’ poverty likelihoods.

Of course, the relationship between indicators and poverty changes as time passes, so the Mali scorecard applied after 2000 (as it is in practice) is generally biased. Still, unbiasedness is a desirable quality for an estimator.

How accurate are estimates of poverty likelihoods? To measure, the scorecard is applied to 1,000 bootstrap samples of size $n = 16,384$ from the validation sub-sample.

Bootstrapping entails:⁵

- Score each household in the validation sample
- Draw a new sample *with replacement* from the validation sample
- For each score, compute the true poverty likelihood in the bootstrap sample, that is, the share of households with the score and with expenditure below a poverty line
- For each score, record the difference between the estimated poverty likelihood from Figure 4 and the true poverty likelihood in the bootstrap sample
- Repeat the previous three steps 1,000 times
- For each score, report the average difference between estimated and true poverty likelihoods across the 1,000 bootstrap samples
- For each score, report the two-sided interval containing the central 900, 950, or 990 differences between estimated and true poverty likelihoods

For the 20 score ranges, Figure 7 shows the average difference between estimated and true poverty likelihoods as well as confidence intervals for the differences. For the national line, the average poverty likelihood across bootstrap samples for scores of 5–9 in the validation sample is too low by 13.1 percentage points. For scores of 50–54, the estimate is too low by 1.1 percentage points.

The 90-percent confidence interval for the differences for scores of 50–54 is $+/-$ 2.5 percentage points (Figure 7).⁶ This means that in 900 of 1,000 bootstraps, the difference between the estimate and the true value is between -3.6 and 1.4 percentage

⁵ Efron and Tibshirani, 1993.

⁶ Confidence intervals are a standard, widely understood measure of precision.

points (because $-1.1 - 2.5 = -3.6$, and $-1.1 + 2.5 = 1.4$). In 950 of 1,000 bootstraps (95 percent), the difference is -1.1 ± 2.9 percentage points, and in 990 of 1,000 bootstraps (99 percent), the difference is -1.1 ± 3.9 percentage points.

For almost all score ranges, Figure 7 shows differences—sometimes large ones—between estimated poverty likelihoods and true values. This is because the validation sub-sample is a single sample that—thanks to sampling variation—differs in distribution from the construction/calibration sub-samples and from Mali’s population. For targeting, however, what matters is less accuracy in all score ranges and more accuracy in score ranges just above and below the targeting cut-off. This fact mitigates the effects of bias and sampling variation on targeting (Friedman, 1997). Section 9 below looks at targeting accuracy in detail.

Of course, if estimates of groups’ poverty rates are to be usefully accurate, then errors for individual households must largely cancel out. As discussed later, this is generally what happens.

Figure 8 (summarizing Figure 9 across poverty lines) shows that absolute differences, when averaged across score ranges for a given poverty line, are less than 2.0 percentage points. These differences are due to sampling variation.

There are three approaches to mitigating differences between estimated and true values. First, poverty likelihoods in application could be adjusted to compensate for the differences in Figure 7. For the example of scores of 50–54, the associated poverty likelihood would not be 47.4 percent from Figure 4 but rather this figure adjusted for

the -1.1 percentage-point average difference from Figure 7, that is, $47.4 - (-1.1) = 48.5$ percent.

A second approach to mitigating differences between estimates and true values is to increase the fineness of the points (for example, by making them 0–200 instead of 0–100) or to increase the number of ranges into which scores are grouped (for example, 40 instead of 20). But this adds complexity, and experiments suggest that while grouping scores and rounding points do matter, they are not the main sources of differences.

By construction, the scorecard here is unbiased for the 2001 EMEP. But it may still be *overfit* when applied after 2001. That is, it may fit the 2001 data so closely that it captures not only timeless patterns but also some random patterns that, due to sampling variation, show up only in 2001. Or the scorecard may be overfit in that it becomes biased as the relationship between indicators and poverty changes over time.

Overfitting can be mitigated by simplifying the scorecard and by not relying only on data but rather also considering experience, judgment, and theory. Of course, the scorecard here does this. Bootstrapping can also mitigate overfitting by reducing (but not eliminating) dependence on a single sampling instance. Combining scorecards can also help, but that would increase complexity too much in this context.

The third approach is to do nothing. After all, most errors in individual households' likelihoods cancel out in the estimates of groups' poverty rates (see later sections). Also, further simplification of the scorecard probably has limited returns.

7. Estimates of a group's poverty rate at a point in time

A group's estimated poverty rate at a point in time is the average of the estimated poverty likelihoods of the individual households in the group.

To illustrate, suppose a program samples three households on Jan. 1, 2008 and that they have scores of 20, 30, and 40, corresponding to poverty likelihoods of 94.1, 86.3, and 81.5 percent (national line, Figure 4). The group's estimated poverty rate is the households' average poverty likelihood of $(94.1 + 86.3 + 81.5) \div 3 = 87.3$ percent.⁷

7.1 Accuracy of estimated poverty rates at a point in time

How accurate is this estimate? For a range of sample sizes, Figure 11 reports average differences between estimated and true poverty rates as well as precision (average confidence intervals for the differences) for the scorecard applied to 1,000 bootstrap samples from the validation sample. For the national line and sample sizes of more than about $n = 256$, the scorecard is too low by 1.6 percentage points; it estimates a poverty rate of 56.8 percent for the validation sample when the true value is 58.4 percent (Figure 2). For all poverty lines, absolute differences for the validation sample average about 2.7 percentage points (Figure 10), ranging from -0.7 percentage points for \$2/day to 5.0 percentage points for \$3/day.

⁷ The group's poverty rate is *not* the poverty likelihood associated with the average score. Here, the average score is $(20 + 30 + 40) \div 3 = 30$, and the poverty likelihood associated with the average score is 86.3 percent. This is not the 87.3 percent found as the average of the three poverty likelihoods associated with each of the three scores.

As before, these differences are due to sampling variation in the validation sample and in the random division of the 2001 EMEP into three sub-samples.

In terms of precision, the 90-percent confidence interval for a group's estimated poverty rate at a point in time and $n = 16,384$ is 1.0 percentage points or less (Figure 10). This means that in 900 of 1,000 bootstraps of this size, the difference between the estimate and the true value is within 1.0 percentage points of the average difference. In the specific example of the national line and the validation sample, 90 percent of all samples of $n = 16,384$ produce estimates that differ from the true value in the range of $-1.6 - 0.6 = -2.2$ to $-1.6 + 0.6 = -1.0$ percentage points. (In this case, -1.6 is the average difference, and ± 0.6 is the 90-percent confidence interval.)

7.2 Sample-size formula for estimates of poverty rates at a point in time

How many households should an organization sample if it wants to estimate their poverty rate at a point in time for a desired confidence interval and confidence level? This practical question was first addressed in Schreiner (2008b).⁸

⁸ IRIS Center (2007a and 2007b) says that $n = 300$ is sufficient for USAID reporting. If a scorecard is as precise as direct measurement, if the expected (before measurement) poverty rate is 50 percent, and if the confidence level is 90 percent, then $n = 300$ implies a confidence interval of ± 2.2 percentage points. In fact, USAID has not specified confidence levels or intervals. Furthermore, the expected poverty rate may not be 50 percent, and the scorecard could be more or less precise than direct measurement.

With direct measurement, the poverty rate can be estimated as the number of households observed to be below the poverty line, divided by the number of all observed households. The formula for sample size n in this case is (Cochran, 1977):

$$n = \left(\frac{z}{c} \right)^2 \cdot \hat{p} \cdot (1 - \hat{p}), \quad (1)$$

where

$$z \text{ is } \begin{cases} 1.64 \text{ for confidence levels of 90 percent} \\ 1.96 \text{ for confidence levels of 95 percent} \\ 2.58 \text{ for confidence levels of 99 percent} \end{cases},$$

c is the confidence interval as a proportion
(for example, 0.02 for an interval of ± 2 percentage points), and

\hat{p} is the expected (before measurement) proportion of households
below the poverty line.

Poverty scorecards, however, do not measure poverty directly, so this formula is not applicable. To derive a similar sample-size formula for Mali, consider the scorecard applied to the validation sample. Figure 2 shows that the expected (before measurement) poverty rate \hat{p} for the national line is 0.568 (that is, the average poverty rate in the construction and calibration sub-samples). In turn, a sample size $n = 16,384$ and a 90-percent confidence level correspond to a confidence interval of ± 0.56 percentage points (Figure 11).⁹ Plugging these into the direct-measurement sample-size formula (1) above gives not $n = 16,384$ but rather $n = \left(\frac{1.64}{0.0056} \right)^2 \cdot 0.568 \cdot (1 - 0.568) =$

⁹ Due to rounding, Figure 11 displays 0.6, not 0.56.

21,045. The ratio of this sample size for scoring (derived empirically via the bootstrap) to the sample size for direct measurement (derived from theory) is $16,384 \div 21,045 = 0.78$.

Applying the same method to $n = 8,192$ (confidence interval of ± 0.79 percentage points) gives $n = \left(\frac{1.64}{0.0079}\right)^2 \cdot 0.568 \cdot (1 - 0.568) = 10,575$. This time, the ratio of the sample size using scoring to the sample size using direct measurement is $8,192 \div 10,575 = 0.77$. This ratio of 0.77 for $n = 8,192$ is close to the ratio of 0.78 for $n = 16,384$. Indeed, applying this same procedure for all $n \geq 256$ in Figure 11 gives ratios that average to 0.76. This can be used to define a sample-size formula for the Mali poverty scorecard applied to the 2001 population:

$$n = \alpha \cdot \left(\frac{z}{c}\right)^2 \cdot \hat{p} \cdot (1 - \hat{p}), \quad (2)$$

where $\alpha = 0.76$ and z , c , and \hat{p} are defined as in (1) above. It is this α that appears in Figure 10 under “ α for sample size”.

To illustrate the use of (2), suppose $c = 0.021$ (confidence interval of ± 2.1 percentage points) and $z = 1.64$ (90-percent confidence). Then (2) gives

$$n = 0.76 \cdot \left(\frac{1.64}{0.021}\right)^2 \cdot 0.568 \cdot (1 - 0.568) = 1,138, \text{ which is close to the sample size of } 1,024 \text{ for}$$

these parameters in Figure 11.

If the sample-size factor α is less than 1.0, then the scorecard is more precise than direct measurement. This occurs for two of six poverty lines in Figure 10.

Of course, the sample-size formulas here are specific to Mali, its poverty lines, its poverty rates, and this scorecard. The derivation method, however, is valid for any poverty scorecard following the approach in this paper.

In practice after 2001, an organization would select a poverty line (say, \$1/day), select a desired confidence level (say, 90 percent, or $z = 1.64$), select a desired confidence interval (say, ± 2 percentage points, or $c = 0.02$), make an assumption about \hat{p} (perhaps based on a previous measurement such as the 25.4 percent national average for 2001, Figure 2), look up α (here, 2.67 for \$1/day), assume that the scorecard will still work after 2001,¹⁰ and then compute the required sample size. In this

illustration, $n = 2.67 \cdot \left(\frac{1.64}{0.02}\right)^2 \cdot 0.254 \cdot (1 - 0.254) = 3,402$.

If the scorecard has already been applied to a sample n , then \hat{p} is the scorecard's estimated poverty rate and the confidence interval c is $\pm z \cdot \sqrt{\frac{\alpha \cdot \hat{p} \cdot (1 - \hat{p})}{n}}$.

¹⁰ This paper reports accuracy for the scorecard applied to the 2001 validation sample, but it cannot test accuracy for later years. Still, performance after 2001 will probably resemble that in 2001, with some deterioration as time passes.

8. Estimates of changes in group poverty rates over time

The change in a group's poverty rate between two points in time is estimated as the change in the average poverty likelihood of the households in the group.

8.1 Warning: Change is not impact

Scoring can estimate change. Of course, change could be for the better or for the worse, and scoring does not indicate what caused change. This point is often forgotten or confused, so it bears repeating: poverty scoring simply estimates change, and it does not, in and of itself, indicate the reason for the change. In particular, estimating the impact of program participation requires knowing what would have happened to participants if they had not been participants (Moffitt, 1991). Knowing this requires either strong assumptions or a control group that resembles participants in all ways except participation. To belabor the point, poverty scoring can help estimate program impact only if there is some way to know what would have happened in the absence of the program. And that information must come from somewhere beyond poverty scoring. Even measuring simple change usually requires the strong assumptions about the constancy of population and about the randomness of program drop-outs.

8.2 Calculating estimated changes in poverty rates over time

Consider the illustration begun in the previous section. On Jan. 1, 2008, a program samples three households who score 20, 30, and 40 and so have poverty

likelihoods of 94.1, 86.3, and 81.5 percent (national line, Figure 4). The group's baseline estimated poverty rate is the households' average poverty likelihood of $(94.1 + 86.3 + 81.5) \div 3 = 87.3$ percent.

In the follow-up round after baseline, two sampling approaches are possible:

- Score a new, independent sample, measuring change by cohort across the samples
- Score the same sample at follow-up as at baseline

By way of illustration, suppose that a year later on Jan. 1, 2009, the program samples three additional households who are in the same cohort as the three original households (or suppose that the program scores the original households a second time) and gets scores of 25, 35, and 45 (poverty likelihoods of 89.4, 76.4, and 63.9 percent, national line, Figure 4). The average poverty likelihood at follow-up is now $(89.4 + 76.4 + 63.9) \div 3 = 76.6$ percent, an improvement of $87.3 - 76.6 = 10.7$ percentage points.

This suggests that about one in ten participants crossed the poverty line in 2008.¹¹ Among those who started below the line, about one in eight ($10.7 \div 87.3 = 12.3$ percent) ended up above the line.¹²

8.3 Accuracy for estimated change

Data is available for Mali only for 2001, so it is not possible to measure the accuracy of scorecard estimates of changes in groups' poverty rates over time.

¹¹ This is a net figure; some people start above the line and end below it, and vice versa.

¹² Poverty scoring does not reveal the reasons for this change.

In practice, of course, Mali’s poverty scorecard can still be applied to estimate change. The following sub-sections suggest approximate sample-size formula that may be used until a new nationally representative expenditure survey is available.

Under direct measurement, the sample-size formula for estimates of changes in poverty rates in two equal-sized independent samples is:

$$n = 2 \cdot \left(\frac{z}{c} \right)^2 \cdot \hat{p} \cdot (1 - \hat{p}), \quad (3)$$

where z , c , and \hat{p} are defined as in (1). Before measurement, \hat{p} is assumed equal at baseline and follow-up. n is the sample size at both baseline and follow-up.¹³

The method developed in the previous section can be used again to derive a sample-size formula for indirect measurement via poverty scoring:

$$n = \alpha \cdot 2 \cdot \left(\frac{z}{c} \right)^2 \cdot \hat{p} \cdot (1 - \hat{p}). \quad (4)$$

For Peru and India (Schreiner, 2008b and 2008c), the average α across poverty lines is 1.6 and 1.2, so 1.5 may be a reasonable figure for Mali.

To illustrate the use of (4), suppose the confidence level is 90 percent ($z = 1.64$), the confidence interval is 2 percentage points ($c = 0.02$), the poverty line is \$1/day, $\alpha = 1.5$, and $\hat{p} = 0.254$ (Figure 2). Then baseline sample size is

$$n = 1.5 \cdot 2 \cdot \left(\frac{1.64}{0.02} \right)^2 \cdot 0.254 \cdot (1 - 0.254) = 3,823, \text{ and follow-up sample size is also } 3,823.$$

¹³ This means that, for a given precision and with direct measurement, estimating the change in a poverty rate between two points in time requires four times as many measurements (not twice as many) as does estimating a poverty rate at a point in time.

8.4 Accuracy for estimated change for one sample, scored twice

The direct-measurement sample-size formula for one sample, scored twice is:¹⁴

$$n = \left(\frac{z}{c}\right)^2 \cdot [\hat{p}_{12} \cdot (1 - \hat{p}_{12}) + \hat{p}_{21} \cdot (1 - \hat{p}_{21}) + 2 \cdot \hat{p}_{12} \cdot \hat{p}_{21}], \quad (5)$$

where z and c are defined as in (1), \hat{p}_{12} is the expected (before measurement) share of all sampled cases that move from below the poverty line to above it, and \hat{p}_{21} is the expected share of all sampled cases that move from above the line to below it.

How can a user set \hat{p}_{12} and \hat{p}_{21} ? Before measurement, a reasonable assumption is that the net change in the poverty rate is zero. Then $\hat{p}_{12} = \hat{p}_{21} = \hat{p}_*$, and (5) becomes:

$$n = 2 \cdot \left(\frac{z}{c}\right)^2 \hat{p}_*. \quad (6)$$

Still, \hat{p}_* could be anything between 0–1, so (6) is not enough to compute sample size. The estimate of \hat{p}_* must be based on data available before baseline measurement.

Suppose that the observed relationship between \hat{p}_* and the variance of the baseline poverty rate $p_{baseline} \cdot (1 - p_{baseline})$ is—as in Peru, see Schreiner (2008b)—close to $\hat{p}_* = 0.0085 + 0.206 \cdot [p_{baseline} \cdot (1 - p_{baseline})]$. Of course, $p_{baseline}$ is not known before baseline measurement, but it is reasonable to use as its expected value a previously observed poverty rate. Given this and a poverty line, a sample-size formula for a single sample directly measured twice for Mali after 2001 is:

¹⁴ See McNemar (1947) and Johnson (2007). John Pezzullo helped find this formula.

$$n = 2 \cdot \left(\frac{z}{c}\right)^2 \cdot \{0.0085 + 0.206 \cdot [p_{2001} \cdot (1 - p_{2001})]\}. \quad (7)$$

As usual, (7) is multiplied by α to get scoring's sample-size formula:

$$n = \alpha \cdot 2 \cdot \left(\frac{z}{c}\right)^2 \cdot \{0.0085 + 0.206 \cdot [p_{2001} \cdot (1 - p_{2001})]\}. \quad (8)$$

In Peru (the only other country for which there is an estimate), the average α across years and poverty lines is about 1.8.

To illustrate, suppose the desired confidence level is 90 percent ($z = 1.64$), the desired confidence interval is 2 percentage points ($c = 0.02$), the poverty line is \$1/day, and the sample is first scored in 2008. The before-baseline poverty rate is 25.4 percent ($p_{2001} = 0.254$, Figure 2), and suppose $\alpha = 1.8$. Then baseline sample size is

$$n = 1.8 \cdot 2 \cdot \left(\frac{1.64}{0.02}\right)^2 \cdot \{0.0085 + 0.206 \cdot [0.254 \cdot (1 - 0.254)]\} = 1,151. \text{ Of course, the same group}$$

of 1,151 households are scored at follow-up as well.

For a given confidence level and confidence interval, sample sizes are smaller when one sample is scored twice than when there are two independent samples.

9. Targeting

When a program uses poverty scoring for targeting, households with scores at or below a cut-off are labeled *targeted* and treated—for program purposes—as if they are below a given poverty line. Households with scores above a cut-off are *non-targeted* and treated—for program purposes—as if they are above a given poverty line.

There is a distinction between *targeting status* (scoring at or below a targeting cut-off) and *poverty status* (expenditure below a poverty line). Poverty status is a fact that depends on whether expenditure is below a poverty line as directly measured by a survey. In contrast, targeting status is a program’s policy choice that depends on a cut-off and on an indirect estimate from a scorecard.

Targeting is successful when households truly below a poverty line are targeted (*inclusion*) and when households truly above a poverty line are not targeted (*exclusion*). Of course, no scorecard is perfect, and targeting is unsuccessful when households truly below a poverty line are not targeted (*undercoverage*) or when households truly above a poverty line are targeted (*leakage*). Figure 12 depicts these four targeting outcomes. Targeting accuracy varies by cut-off; a higher cut-off has better inclusion (but worse leakage), while a lower cut-off has better exclusion (but worse undercoverage).

A program should weigh these trade-offs when setting a cut-off. A formal way to do this is to assign net benefits—based on a program’s values and mission—to each of the four possible targeting outcomes and then to choose the cut-off that maximizes total net benefits (Adams and Hand, 2000; Hoadley and Oliver, 1998).

Figure 13 shows the distribution of households by targeting outcome for Mali’s scorecard applied to the validation sample. For an example cut-off of 50–54, outcomes for the national line are:

- Inclusion: 53.1 percent are below the line and correctly targeted
- Undercoverage: 5.2 percent are below the line and mistakenly not targeted
- Leakage: 15.5 percent are above the line and mistakenly targeted
- Exclusion: 26.1 percent are above the line and correctly not targeted

Increasing the cut-off to 55–59 improves inclusion and undercoverage but worsens leakage and exclusion:

- Inclusion: 55.6 percent are below the line and correctly targeted
- Undercoverage: 2.8 percent are below the line and mistakenly not targeted
- Leakage: 21.8 percent are above the line and mistakenly targeted
- Exclusion: 19.9 percent are above the line and correctly not targeted

Which cut-off is preferred depends on total net benefit. If each targeting outcome has a per-household benefit or cost, then total net benefit for a given cut-off is:

Benefit per household correctly included	x	Households correctly included	+
Cost per household mistakenly not covered	x	Households mistakenly not covered	+
Cost per household mistakenly leaked	x	Households mistakenly leaked	+
Benefit per household correctly excluded	x	Households correctly excluded.	

To set an optimal cut-off, a program would:

- Assign benefits and costs to possible outcomes, based on its values and mission
- Tally total net benefits for each cut-off using Figure 13 for a poverty line
- Select the cut-off with the highest total net benefit

The most difficult step is assigning benefits and costs to targeting outcomes. Any program that uses targeting—with or without scoring—should thoughtfully consider how it values successful inclusion or exclusion versus errors of undercoverage and

leakage. It is healthy to go through a process of thinking explicitly and intentionally about how possible targeting outcomes are valued.

A common choice of benefits and costs is “Total Accuracy” (IRIS, 2005; Grootaert and Braithwaite, 1998). With this criterion, total net benefit is the number of households correctly included or excluded:

$$\begin{array}{rclcl}
 \text{Total Accuracy} = & 1 & \times & \text{Households correctly included} & + \\
 & 0 & \times & \text{Households mistakenly undercovered} & + \\
 & 0 & \times & \text{Households mistakenly leaked} & + \\
 & 1 & \times & \text{Households correctly excluded.} &
 \end{array}$$

Figure 13 shows “Total Accuracy” for all cut-offs for the Mali scorecard. For the national line and the validation sample, total net benefit is greatest (84.1) for a cut-off of 45–49, with about four in five households correctly classified.

“Total Accuracy” weighs successful inclusion of households below the line the same as successful exclusion of households above the line. If a program valued inclusion more (say, twice as much) than exclusion, it could reflect this by setting the benefit for inclusion to 2 and the benefit for exclusion to 1. Then the chosen cut-off would maximize $(2 \times \text{Households correctly included}) + (1 \times \text{Households correctly excluded})$.

IRIS (2005) proposes a new criterion called the “Balanced Poverty Accuracy Criterion”. BPAC considers two goals:¹⁵

- Inclusion
- Unbiasedness of the estimated poverty rate

¹⁵ A criterion must consider at least two outcomes among inclusion, undercoverage, leakage, and exclusion. If not, it would imply targeting everyone or no one.

For scorecards that estimate expenditure rather than poverty likelihood, the second goal is optimized by minimizing the absolute value of the difference between undercoverage and leakage. After normalizing by the number of households below the poverty line, the BPAC formula is

$$(\text{Inclusion} + |\text{Undercoverage} - \text{Leakage}|) \times [100 \div (\text{Inclusion} + \text{Undercoverage})].$$

BPAC is mostly relevant for poverty scorecards that estimate expenditure rather than poverty likelihood. In this case, the difference between an estimated poverty rate and the true value is equal to the difference between undercoverage and leakage.

BPAC is less relevant, however, for scorecards—like the one here—that estimate poverty likelihoods. In this case, a group’s estimated poverty rate is the average of its members’ poverty likelihoods, and this is independent of undercoverage and leakage (which in any case depend on a program-selected cut-off).

As an alternative to assigning benefits and costs to targeting outcomes and then choosing a cut-off to maximize total net benefit, a program could set a cut-off to achieve a desired poverty rate among targeted households. Figure 14 shows, for the Mali scorecard applied to the validation sample, the expected poverty rate among households who score at or below a given cut-off. For the example of the national line, targeting households who score 50–54 or less would target 68.6 of all households and produce a poverty rate among those targeted of 77.4 percent.¹⁶

¹⁶ If potential participants are not representative of all of Mali, then Figure 14 is valid only if selection into potential participation—whether by the program or potential participant—is unrelated with poverty in any way not captured by the scorecard.

10. Conclusion

This paper presents a simple poverty scorecard for Mali that can be used to estimate the likelihood that a household has expenditure below a given poverty line, to estimate the poverty rate of a group of households at a point in time, and to estimate changes in the poverty rate of a group of households between two points in time. The scorecard can also be used for targeting.

The scorecard is inexpensive to use and can be understood by non-specialists. It is designed to be practical for local pro-poor organizations who want to improve how they monitor and manage their social performance so as to speed up their participants' progress out of poverty.

The scorecard is built with a sub-sample of data from Mali's 2001 EMEP, tested with a different sub-sample, and calibrated to six poverty lines (national, food, USAID "extreme", \$1/day, \$2/day, and \$3/day).

Accuracy and sample-size formulas are reported for estimates of households' poverty likelihoods, groups' poverty rates at a point in time, and changes in groups' poverty rates over time. Of course, the scorecard's estimates of changes in poverty rates are not the same as estimates of program impact.

When the scorecard is applied to the validation sample, the difference between estimates versus true poverty rates for groups of households at a point in time averages—across the six poverty lines—about 2.7 percentage points. For $n = 16,384$

and 90-percent confidence, these differences are precise to ± 1.0 percentage points or less, and for $n = 1,024$, precision is ± 4.0 percentage points or less.

For targeting, programs can use the results reported here to select a cut-off that fits their values and mission.

Although the statistical technique is innovative, and although technical accuracy is important, the design of the scorecard here focuses on transparency and ease-of-use. After all, a perfectly accurate scorecard is worthless if programs feel so daunted by its complexity or its cost that they do not even try to use it. For this reason, the poverty scorecard is kept simple, using 10 indicators that are inexpensive to collect and that are straightforward to verify. Points are all zeros or positive integers, and scores range from 0 (most likely below a poverty line) to 100 (least likely below a poverty line). Scores are related to poverty likelihoods via simple look-up tables, and targeting cut-offs are likewise simple to apply. The design attempts to facilitate adoption by helping managers understand and trust scoring and by allowing non-specialists to generate scores quickly in the field.

In sum, the poverty scorecard is a practical, objective way for pro-poor programs in Mali to monitor poverty rates, track changes in poverty rates over time, and target services. The same approach can be applied to any country with similar data from a national expenditure survey.

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Figure 2: Sample sizes and household poverty rates by sub-sample and poverty line

Sub-sample	Poverty rate	# surveyed	% with expenditure below a poverty line					
			National	National Food	USAID 'Extreme'	International \$1/day	International \$2/day	International \$3/day
Poverty line (Fcfa/person/day)		—	395	271	228	215	431	646
Construction								
Selecting indicators and weights	Households	1,739	57.1	36.8	27.6	24.4	61.1	79.4
	People	—	67.3	48.3	37.6	34.1	70.7	85.8
Calibration								
Associating scores with likelihoods	Households	1,755	56.5	36.8	27.6	24.7	60.8	80.8
	People	—	68.1	48.7	39.2	36.1	72.2	87.2
Validation								
Testing accuracy	Households	1,807	58.4	40.2	30.6	27.1	63.2	80.0
	People	—	69.3	52.5	41.9	38.1	73.2	87.3
All Mali								
	Households	5,301	57.3	38.0	28.6	25.4	61.7	80.1
	People	—	68.2	49.9	39.6	36.1	72.0	86.8

Source: 2001 EMEP.

Figure 3: Poverty indicators by uncertainty coefficient

<u>Uncertainty coefficient</u>	<u>Indicator (Answers ordered starting with those most strongly indicative of poverty)</u>
2000	How many household members have agriculture/animal husbandry/fishing/forestry as their principal occupation? (Three or more; Two; One or none)
1592	How many household members are paid in kind in their principal employment? (Five or more; Two, three, or four; One; None)
1361	How many household members are self-employed in their principal occupation? (Five or more; Four; Three; Two; One; None)
1270	What is the main construction material of the floor of the residence? (Packed earth, or other; Cement or tile)
1104	What is the main source of drinking water? (Surface water, non-modern well, drilled well, or other; Modern well; Public pump; Faucet tap)
1011	Does the household own any plows? (Yes; No)
986	How many household members are 11 years old or younger? (Five or more; Four; Three; Two; One; None)
965	How many household members are 14 years old or younger? (Seven or more; Five or six; Three or four; One or two; None)
960	What is the highest grade that the male head/spouse has completed? (None; No male head/spouse, or first to fifth grade; Sixth to ninth grade; Secondary or superior)
924	What is the highest educational qualification that the male head/spouse has received? (None; No male head/spouse; CEP or DEF; BAC, DEUG, <i>licence</i> , <i>maîtrise</i> or DEA, doctorate, other university degree, CAP, BT, BTS, other degrees)
895	What is the main construction material of the walls of the residence? (Partly cement, or other; Cement)
824	How many household members are 17 years old or younger? (Seven or more; Five or six; Three or four; One or two; None)
806	Does the household own any television sets? (No; Yes)

Figure 3 (continued): Poverty indicators by uncertainty coefficient

<u>Uncertainty coefficient</u>	<u>Indicator (Answers ordered starting with those most strongly indicative of poverty)</u>
797	Does the male head/spouse know how to read and write a simple sentence in some language? (No; No male head/spouse; Yes)
794	What is the tenancy status of the household? (Co-owner with household members; Owner without land title; Owner with land title; Renter, hire/purchase or rent-to-own, free lodging, or other)
778	How many household members are 20 years old or younger? (Eight or more; Five, six, or seven; Four; None, one, two, or three)
763	How many household members are 25 years old or younger? (Ten or more, Eight or nine, Five, six, or seven; Three or four; None, one, or two)
672	Do all children ages 6 to 12 attend school? (No; No children these ages; Yes)
672	What is the highest grade that the female head/spouse has completed? (None, or first grade; Second grade, or no female head/spouse; Third grade or higher)
670	What is the highest educational qualification that any household member has received? (None; CEP; DEF; BAC, DEUG, <i>licence</i> , <i>maîtrise</i> or DEA, doctorate, other university degree, CAP, BT, BTS, other degrees)
670	How many household members are there? (Ten or more; Five to Nine; One to Four)
637	What is the highest grade completed by any household member? (None, or first to fifth grade; Sixth to ninth grade; Secondary or superior)
612	Do all children ages 6 to 11 attend school? (No; No children these ages; Yes)
607	What is the main source of lighting for the residence? (Kerosene/paraffin lamp, or other; Gas lamp, solar energy, or generator; Electricity)
578	How many household members are 35 years old or younger? (Nine or more, Seven or eight; Three to six; None, one, or two)
573	What is the highest educational qualification that the female head/spouse has received? (None; No female head/spouse; Any other educational qualification)

Figure 3 (continued): Poverty indicators by uncertainty coefficient

<u>Uncertainty coefficient</u>	<u>Indicator (Answers ordered starting with those most strongly associated with poverty)</u>
569	Do all children ages 6 to 14 attend school? (No; No children these ages; Yes)
565	Does the female head/spouse know how to read and write a simple sentence in some language? (No; No female head/spouse; Yes)
550	How many household members work in salaried jobs as their principal occupation? (None; One or more)
539	Does the household own any fans? (No; Yes)
480	Do all children ages 6 to 19 attend school? (No; No children these ages; Yes)
464	Does the household own any radios? (No; Yes)
446	Do all children ages 6 to 17 attend school? (No; No children these ages; Yes)
445	How many household members are self-employed as their profession? (None; One or more)
411	How many household members know how to read and write a simple sentence in some language? (None; One; Two; Three; Four or more)
405	What toilet arrangements does the household have? (Other; Private or shared latrine or flush toilet inside or outside house)
381	What is the marital status of the male head/spouse? (Married, polygamous; Married, monogamous; Single, or no male head/spouse; Widowed, divorced, or separated)
377	What kind of residence does the household have? (Country house, shack, or other; Lodging house; Modern detached house or apartment)
323	What is the main construction material of the roof of the residence? (Tile or thatch; Mud, corrugated metal sheets, concrete, or other)
315	What is the age of the male head/spouse? (65 or older; 36 to 64; 34 or younger; No male head/spouse)
314	What is the marital status of the female head/spouse? (Single; Married, polygamous or monogamous; Widowed, divorced, or separated; No female head/spouse)
308	Do all children ages 6 to 11 attend school? (No; No children these ages; Yes)
281	Does the household own any handcarts? (Yes; No)

Figure 3 (continued): Poverty indicators by uncertainty coefficient

<u>Uncertainty coefficient</u>	<u>Indicator (Answers ordered starting with those most strongly associated with poverty)</u>
238	Does the household own any bicycles? (Yes; No)
237	Does the household own any pumps for cotton (No; Yes)
232	Does the household own any irons? (No; Yes)
206	What is the main fuel for cooking? (Electricity, kerosene, firewood, or other; Charcoal or gas)
199	What is the structure of household headship? (Male and female heads/spouses; No female head/spouse; No male head/spouse)
189	Does the household own any handcarts, bicycles, or motorbikes? (Yes; No)
187	Does the household own any motorbikes? (No; Yes)
143	How many household members attend a private or religious school? (None; One or more)
131	Is there a kitchen? (Yes; No)
121	How many rooms does the household occupy? (Five or more; One to four)
100	What is the age of the female head/spouse? (55 or older; 25 to 54; 24 or younger; No female haed/spouse)
92	Does the household own any stoves? (No; Yes)
71	Does the household own any improved wood-burning stoves? (No; Yes)
38	Does the household own any harrows? (Yes; No)
18	Does the household own any fishing nets? (Yes; No)
1	Is there a storage room? (No; Yes)

Source: 2001 EMEP.

National Poverty Line Tables
(and tables pertaining to all poverty lines)

Figure 4 (National poverty line): Estimated poverty likelihoods associated with scores

If an individual's score is then the likelihood (%) of being below the poverty line is:
0-4	100.0
5-9	86.9
10-14	98.4
15-19	94.2
20-24	94.1
25-29	89.4
30-34	86.3
35-39	76.4
40-44	81.5
45-49	63.9
50-54	47.4
55-59	24.9
60-64	21.3
65-69	7.2
70-74	5.6
75-79	6.7
80-84	0.8
85-89	0.0
90-94	5.9
95-100	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 5 (National poverty line): Derivation of estimated poverty likelihoods associated with scores

Score	People below poverty line		All people at score		Poverty likelihood (estimated, %)
0-4	286	÷	286	=	100.0
5-9	262	÷	302	=	86.9
10-14	2,541	÷	2,582	=	98.4
15-19	3,507	÷	3,725	=	94.2
20-24	3,598	÷	3,825	=	94.1
25-29	9,505	÷	10,638	=	89.4
30-34	7,083	÷	8,210	=	86.3
35-39	10,328	÷	13,527	=	76.4
40-44	9,304	÷	11,414	=	81.5
45-49	3,892	÷	6,093	=	63.9
50-54	3,807	÷	8,033	=	47.4
55-59	2,180	÷	8,760	=	24.9
60-64	1,274	÷	5,975	=	21.3
65-69	382	÷	5,327	=	7.2
70-74	245	÷	4,386	=	5.6
75-79	197	÷	2,965	=	6.7
80-84	19	÷	2,379	=	0.8
85-89	0	÷	846	=	0.0
90-94	28	÷	477	=	5.9
95-100	0	÷	251	=	0.0

Number of households normalized to sum to 100,000.

Based on the 2001 EMEP.

Figure 6 (All poverty lines): Distribution of poverty likelihoods across poverty ranges, by score

Score	Likelihood expenditure is between two adjacent poverty lines				
		=>\$1/day	=>Food	=>National	=>\$3/day
	<\$1/day	and	and	and	
		<Food	<National	<\$3/day	
	=>Fcfa215	=>Fcfa271	=>Fcfa395	=>Fcfa646	
	and	and	and		
	<Fcfa271	<Fcfa395	<Fcfa646		
0-4	72.8	0.0	27.2	0.0	0.0
5-9	86.9	0.0	0.0	13.1	0.0
10-14	71.2	9.9	17.4	1.6	0.0
15-19	66.8	10.0	17.4	5.8	0.0
20-24	60.4	17.4	16.3	5.5	0.4
25-29	50.3	21.4	17.7	8.5	2.1
30-34	58.3	16.8	11.3	12.2	1.5
35-39	25.8	19.4	31.2	14.3	9.4
40-44	27.2	18.6	35.7	14.4	4.1
45-49	13.0	23.0	27.9	27.6	8.5
50-54	10.2	8.8	28.4	41.3	11.3
55-59	3.5	5.0	16.4	43.8	31.3
60-64	0.8	4.2	16.3	33.8	44.9
65-69	0.0	0.9	6.3	51.9	40.9
70-74	0.4	0.0	5.2	36.4	58.0
75-79	0.0	0.0	6.7	19.7	73.6
80-84	0.0	0.8	0.0	37.4	61.8
85-89	0.0	0.0	0.0	39.0	61.1
90-94	0.0	0.0	5.9	4.2	90.0
95-100	0.0	0.0	0.0	0.0	100.0

Poverty lines are in units of Fcfa/person/day.

All poverty likelihoods are in percentage units.

USAID "extreme" line is not displayed because it is very close to the \$1/day line.

\$2/day line is not displayed because it is very close to the national line.

Figure 7 (National poverty line): Bootstrapped differences between estimated and true poverty likelihoods for households in a large sample ($n = 16,384$), with confidence intervals, scorecard applied to the validation sample

Scorecard applied to validation sample, difference between estimate and true value				
Score	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
0-4	0.0	0.0	0.0	0.0
5-9	-13.1	6.6	6.6	6.6
10-14	0.8	1.0	1.2	1.7
15-19	-5.0	2.7	2.7	2.8
20-24	8.6	3.3	3.9	4.9
25-29	2.7	1.5	1.7	2.4
30-34	-10.0	5.3	5.4	5.5
35-39	-8.5	4.9	5.0	5.2
40-44	-9.5	5.2	5.2	5.4
45-49	18.0	3.2	3.8	4.5
50-54	-1.1	2.5	2.9	3.9
55-59	15.1	1.1	1.3	1.6
60-64	-10.3	6.7	7.1	7.9
65-69	0.8	1.2	1.4	1.8
70-74	5.2	0.2	0.3	0.4
75-79	0.9	1.7	2.0	2.6
80-84	0.7	0.1	0.1	0.1
85-89	-36.8	23.1	23.8	24.8
90-94	5.9	0.0	0.0	0.0
95-100	0.0	0.0	0.0	0.0

Figure 8 (All poverty lines): Differences and precision of differences for bootstrapped estimates of households' poverty likelihoods from the scorecard applied to the validation sample

	Poverty line					
	National		USAID			
	National	Food	'Extreme'	\$1/day	\$2/day	\$3/day
Estimate minus true value	-1.2	1.1	-1.6	-2.1	-0.6	5.1
Precision of difference	0.5	0.9	0.9	0.9	0.6	0.7

Precision is measured as 90-percent confidence intervals in units of +/- percentage points. Differences and precision of differences estimated from 1,000 bootstraps of size n=16,384.

Figure 9 (National poverty line): Differences and precision of differences for bootstrapped estimates of households' poverty likelihoods, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-0.3	48.9	60.3	72.0
4	0.1	33.7	42.5	54.9
8	-0.6	25.0	30.3	40.6
16	-1.2	17.9	21.5	27.3
32	-1.1	12.5	15.3	19.8
64	-0.9	8.5	10.0	13.1
128	-0.9	5.8	6.8	9.0
256	-1.1	4.3	4.9	6.2
512	-1.1	3.1	3.6	4.4
1,024	-1.2	2.0	2.3	3.1
2,048	-1.2	1.4	1.7	2.3
4,096	-1.2	1.0	1.2	1.6
8,192	-1.2	0.7	0.9	1.1
16,384	-1.2	0.5	0.6	0.8

Figure 10 (All poverty lines): Differences, precision of differences, and sample-size α for bootstrapped estimates of poverty rates for groups of households at a point in time for the scorecard applied to the validation sample

	Poverty line					
	National		USAID			
	National	Food	'Extreme'	\$1/day	\$2/day	\$3/day
Estimate minus true value	-1.6	-0.9	-4.0	-4.1	-0.7	5.0
Precision of difference	0.6	0.9	0.9	0.9	0.5	0.7
α for sample size	0.76	1.94	2.29	2.55	0.76	2.16

Precision is measured as 90-percent confidence intervals in units of +/- percentage points.

Differences and precision of differences estimated from 1,000 bootstraps of size n=16,384.

α is estimated from 1,000 bootstrap samples of n=256, 512, 1,024, 2,048, 4,096, 8,192, and 16,384.

Figure 11 (National poverty line): Differences and precision of differences for bootstrapped estimates of poverty rates for groups of households at a point in time, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-0.3	48.9	60.3	72.0
4	0.1	33.6	41.6	55.2
8	-0.8	24.3	29.4	39.4
16	-1.2	17.2	19.8	26.8
32	-1.3	12.2	14.6	19.6
64	-1.3	8.6	10.1	13.0
128	-1.4	6.1	7.1	8.8
256	-1.5	4.4	5.2	6.9
512	-1.6	3.2	3.8	4.9
1,024	-1.5	2.1	2.6	3.7
2,048	-1.6	1.6	1.9	2.4
4,096	-1.6	1.1	1.3	1.7
8,192	-1.6	0.8	0.9	1.2
16,384	-1.6	0.6	0.7	0.9

Figure 12 (All poverty lines): Possible types of outcomes from targeting by poverty score

		<u>Targeting segment</u>	
		<u>Targeted</u>	<u>Non-targeted</u>
<u>True poverty status</u>	<u>Below poverty line</u>	<u>Inclusion</u> Under poverty line Correctly targeted	<u>Undercoverage</u> Under poverty line Mistakenly non-targeted
	<u>Above poverty line</u>	<u>Leakage</u> Above poverty line Mistakenly targeted	<u>Exclusion</u> Above poverty line Correctly non-targeted

Figure 13 (National poverty line): Households by targeting classification and score, along with “Total Accuracy” and BPAC, scorecard applied to the validation sample

Score	<u>Inclusion:</u>	<u>Undercoverage:</u>	<u>Leakage:</u>	<u>Exclusion:</u>	<u>Total Accuracy</u>	<u>BPAC</u>
	< poverty line correctly targeted	< poverty line mistakenly non-targeted	≥ poverty line mistakenly targeted	≥ poverty line correctly non-targeted	Inclusion + Exclusion	See text
0–4	0.3	58.1	0.0	41.6	41.9	-99.0
5–9	0.6	57.8	0.0	41.6	42.2	-98.0
10–14	3.1	55.3	0.1	41.5	44.6	-89.3
15–19	6.7	51.6	0.2	41.5	48.2	-76.7
20–24	10.2	48.2	0.5	41.1	51.3	-64.2
25–29	19.5	38.9	1.9	39.8	59.3	-30.0
30–34	26.9	31.5	2.7	39.0	65.8	-3.3
35–39	37.5	20.9	5.6	36.0	73.5	38.0
40–44	46.1	12.3	8.4	33.2	79.3	72.4
45–49	49.3	9.1	11.3	30.3	79.6	80.6
50–54	53.1	5.2	15.5	26.1	79.3	73.4
55–59	55.6	2.8	21.8	19.9	75.4	62.6
60–64	57.4	1.0	26.0	15.6	73.0	55.4
65–69	57.9	0.4	30.8	10.9	68.8	47.3
70–74	58.0	0.3	35.1	6.6	64.6	39.9
75–79	58.2	0.1	37.8	3.8	62.0	35.2
80–84	58.2	0.1	40.2	1.4	59.7	31.1
85–89	58.4	0.0	40.9	0.7	59.1	29.9
90–94	58.4	0.0	41.4	0.3	58.6	29.1
95–100	58.4	0.0	41.6	0.0	58.4	28.6

Inclusion, undercoverage, leakage, and exclusion normalized to sum to 100.

Figure 14 (National poverty line): Households below the poverty line and all households, at a given score or at or below a given score cut-off, scorecard applied to the validation sample

Score	People below poverty line (%)		All people (%)	
	At score	At or below score	At score	At or below score
0-4	100.0	100.0	0.3	0.3
5-9	100.0	100.0	0.3	0.6
10-14	96.1	96.8	2.6	3.2
15-19	97.9	97.4	3.7	6.9
20-24	90.8	95.1	3.8	10.7
25-29	87.4	91.2	10.6	21.4
30-34	90.1	90.9	8.2	29.6
35-39	78.1	86.9	13.5	43.1
40-44	75.5	84.5	11.4	54.5
45-49	53.0	81.3	6.1	60.6
50-54	47.8	77.4	8.0	68.6
55-59	28.1	71.8	8.8	77.4
60-64	29.4	68.8	6.0	83.4
65-69	11.0	65.3	5.3	88.7
70-74	1.8	62.3	4.4	93.1
75-79	6.5	60.6	3.0	96.0
80-84	0.6	59.2	2.4	98.4
85-89	15.3	58.8	0.8	99.3
90-94	0.0	58.5	0.5	99.7
95-100	0.0	58.4	0.3	100.0

National Food Poverty Line Tables

Figure 4 (National Food poverty line): Estimated poverty likelihoods associated with scores

If an individual's score is then the likelihood (%) of being below the poverty line is:
0-4	72.8
5-9	86.9
10-14	81.0
15-19	76.8
20-24	77.8
25-29	71.7
30-34	75.0
35-39	45.1
40-44	45.8
45-49	36.0
50-54	19.0
55-59	8.5
60-64	5.0
65-69	0.9
70-74	0.4
75-79	0.0
80-84	0.8
85-89	0.0
90-94	0.0
95-100	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 5 (National Food poverty line): Derivation of estimated poverty likelihoods associated with scores

Score	People below poverty line		All people at score		Poverty likelihood (estimated, %)
0-4	208	÷	286	=	72.8
5-9	262	÷	302	=	86.9
10-14	2,092	÷	2,582	=	81.0
15-19	2,859	÷	3,725	=	76.8
20-24	2,976	÷	3,825	=	77.8
25-29	7,625	÷	10,638	=	71.7
30-34	6,157	÷	8,210	=	75.0
35-39	6,105	÷	13,527	=	45.1
40-44	5,226	÷	11,414	=	45.8
45-49	2,195	÷	6,093	=	36.0
50-54	1,525	÷	8,033	=	19.0
55-59	745	÷	8,760	=	8.5
60-64	301	÷	5,975	=	5.0
65-69	46	÷	5,327	=	0.9
70-74	18	÷	4,386	=	0.4
75-79	0	÷	2,965	=	0.0
80-84	19	÷	2,379	=	0.8
85-89	0	÷	846	=	0.0
90-94	0	÷	477	=	0.0
95-100	0	÷	251	=	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 7 (National Food poverty line): Bootstrapped differences between estimated and true poverty likelihoods for households in a large sample ($n = 16,384$), with confidence intervals, scorecard applied to the validation sample

Scorecard applied to validation sample, difference between estimate and true value				
Score	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
0-4	48.3	9.0	10.7	14.6
5-9	11.4	11.7	13.5	19.0
10-14	28.1	5.8	6.9	8.9
15-19	-13.8	7.8	8.0	8.3
20-24	6.6	3.6	4.4	5.8
25-29	2.0	2.2	2.6	3.6
30-34	-12.1	6.7	6.9	7.1
35-39	7.0	2.5	3.0	3.8
40-44	-7.7	5.4	5.6	6.3
45-49	7.3	2.8	3.3	4.3
50-54	-6.2	4.2	4.4	4.8
55-59	3.9	0.7	0.8	1.0
60-64	-1.9	1.7	1.8	2.2
65-69	-1.6	1.3	1.3	1.5
70-74	0.3	0.1	0.1	0.1
75-79	-2.7	1.9	2.1	2.2
80-84	0.7	0.1	0.1	0.1
85-89	0.0	0.0	0.0	0.0
90-94	0.0	0.0	0.0	0.0
95-100	0.0	0.0	0.0	0.0

Figure 9 (National Food poverty line): Differences and precision of differences for bootstrapped estimates of households' poverty likelihoods, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-0.7	51.1	58.9	73.5
4	0.2	41.1	46.9	61.2
8	-0.7	32.8	37.5	45.8
16	-0.2	25.5	29.0	36.3
32	-0.6	18.5	22.7	27.1
64	0.0	13.3	15.3	19.1
128	0.1	8.6	10.0	12.4
256	0.4	6.4	7.9	10.1
512	0.7	4.6	5.3	7.3
1,024	0.9	3.4	4.2	5.2
2,048	1.1	2.4	2.8	4.0
4,096	1.2	1.6	2.0	2.5
8,192	1.1	1.2	1.4	1.8
16,384	1.1	0.9	1.0	1.3

Figure 11 (National Food poverty line): Differences and precision of differences for bootstrapped estimates of poverty rates for groups of households at a point in time, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-0.7	51.1	58.9	73.5
4	-0.1	40.6	47.2	60.6
8	-1.1	32.7	37.9	44.4
16	-0.7	25.5	29.1	34.3
32	-1.1	17.9	21.6	27.4
64	-0.8	12.5	14.7	19.0
128	-0.8	9.0	10.5	14.6
256	-0.9	7.0	8.2	11.2
512	-0.9	4.8	5.7	7.6
1,024	-0.9	3.4	4.0	5.2
2,048	-0.9	2.4	2.9	3.8
4,096	-0.9	1.7	2.0	2.7
8,192	-0.9	1.2	1.4	2.0
16,384	-0.9	0.9	1.0	1.4

Figure 13 (National Food poverty line): Households by targeting classification and score, along with “Total Accuracy” and BPAC, scorecard applied to the validation sample

Score	Inclusion: < poverty line correctly targeted	Undercoverage: < poverty line mistakenly non-targeted	Leakage: ? poverty line mistakenly targeted	Exclusion: ? poverty line correctly non-targeted	Total Accuracy Inclusion + Exclusion	BPAC See text
0–4	0.1	40.0	0.1	59.7	59.8	-98.9
5–9	0.4	39.8	0.2	59.6	60.0	-97.6
10–14	2.4	37.8	0.8	59.0	61.4	-86.1
15–19	5.6	34.6	1.3	58.5	64.2	-68.8
20–24	8.4	31.8	2.3	57.5	65.9	-52.5
25–29	16.1	24.1	5.3	54.5	70.6	-6.9
30–34	21.9	18.3	7.7	52.1	74.0	28.1
35–39	29.3	10.9	13.8	46.0	75.3	65.7
40–44	34.4	5.8	20.1	39.7	74.1	50.0
45–49	36.3	3.9	24.3	35.5	71.7	39.5
50–54	38.4	1.8	30.2	29.6	67.9	24.7
55–59	39.5	0.7	37.9	21.9	61.3	5.6
60–64	39.9	0.3	43.4	16.4	56.3	-8.1
65–69	40.1	0.1	48.6	11.2	51.2	-21.0
70–74	40.1	0.1	53.0	6.8	46.9	-31.9
75–79	40.2	0.0	55.9	3.9	44.1	-39.0
80–84	40.2	0.0	58.2	1.6	41.8	-44.9
85–89	40.2	0.0	59.1	0.7	40.9	-47.0
90–94	40.2	0.0	59.6	0.3	40.4	-48.2
95–100	40.2	0.0	59.8	0.0	40.2	-48.8

Inclusion, undercoverage, leakage, and exclusion normalized to sum to 100.

Figure 14 (National Food poverty line): Households below the poverty line and all households, at a given score or at or below a given score cut-off, scorecard applied to the validation sample

Score	People below poverty line (%)		All people (%)	
	At score	At or below score	At score	At or below score
0-4	49.2	49.2	0.3	0.3
5-9	79.1	64.6	0.3	0.6
10-14	78.4	75.8	2.6	3.2
15-19	86.6	81.6	3.7	6.9
20-24	72.0	78.2	3.8	10.7
25-29	72.1	75.2	10.6	21.4
30-34	71.1	74.1	8.2	29.6
35-39	54.8	68.0	13.5	43.1
40-44	44.6	63.1	11.4	54.5
45-49	30.6	59.8	6.1	60.6
50-54	26.4	55.9	8.0	68.6
55-59	12.2	51.0	8.8	77.4
60-64	7.9	47.9	6.0	83.4
65-69	2.7	45.2	5.3	88.7
70-74	0.4	43.1	4.4	93.1
75-79	3.1	41.8	3.0	96.0
80-84	0.6	40.8	2.4	98.4
85-89	0.0	40.5	0.8	99.3
90-94	0.0	40.3	0.5	99.7
95-100	0.0	40.2	0.3	100.0

USAID “Extreme” Poverty Line Tables

Figure 4 (USAID “Extreme” poverty line): Estimated poverty likelihoods associated with scores

If an individual's score is then the likelihood (%) of being below the poverty line is:
0–4	72.8
5–9	86.9
10–14	74.7
15–19	72.1
20–24	70.3
25–29	59.7
30–34	61.4
35–39	26.7
40–44	30.6
45–49	18.1
50–54	11.2
55–59	4.0
60–64	2.2
65–69	0.5
70–74	0.4
75–79	0.0
80–84	0.0
85–89	0.0
90–94	0.0
95–100	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 5 (USAID “Extreme” poverty line): Derivation of estimated poverty likelihoods associated with scores

Score	People below poverty line		All people at score		Poverty likelihood (estimated, %)
0–4	208	÷	286	=	72.8
5–9	262	÷	302	=	86.9
10–14	1,928	÷	2,582	=	74.7
15–19	2,685	÷	3,725	=	72.1
20–24	2,689	÷	3,825	=	70.3
25–29	6,350	÷	10,638	=	59.7
30–34	5,038	÷	8,210	=	61.4
35–39	3,610	÷	13,527	=	26.7
40–44	3,487	÷	11,414	=	30.6
45–49	1,105	÷	6,093	=	18.1
50–54	898	÷	8,033	=	11.2
55–59	352	÷	8,760	=	4.0
60–64	131	÷	5,975	=	2.2
65–69	25	÷	5,327	=	0.5
70–74	18	÷	4,386	=	0.4
75–79	0	÷	2,965	=	0.0
80–84	0	÷	2,379	=	0.0
85–89	0	÷	846	=	0.0
90–94	0	÷	477	=	0.0
95–100	0	÷	251	=	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 7 (USAID “Extreme” poverty line): Bootstrapped differences between estimated and true poverty likelihoods for households in a large sample ($n = 16,384$), with confidence intervals, scorecard applied to the validation sample

Scorecard applied to validation sample, difference between estimate and true value				
Score	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
0-4	48.3	9.0	10.7	14.6
5-9	11.4	11.7	13.5	19.0
10-14	24.1	5.8	6.5	8.6
15-19	-12.0	7.2	7.4	7.9
20-24	4.2	3.7	4.6	5.9
25-29	3.6	2.5	3.0	4.0
30-34	-17.9	9.9	10.0	10.3
35-39	5.5	1.7	1.9	2.7
40-44	-17.5	10.3	10.6	11.2
45-49	5.1	1.7	2.1	2.6
50-54	-6.7	4.3	4.5	5.0
55-59	2.3	0.4	0.5	0.6
60-64	0.0	0.7	0.9	1.2
65-69	0.5	0.0	0.0	0.0
70-74	0.3	0.1	0.1	0.1
75-79	0.0	0.0	0.0	0.0
80-84	0.0	0.0	0.0	0.0
85-89	0.0	0.0	0.0	0.0
90-94	0.0	0.0	0.0	0.0
95-100	0.0	0.0	0.0	0.0

Figure 9 (USAID “Extreme” poverty line): Differences and precision of differences for bootstrapped estimates of households’ poverty likelihoods, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-1.2	51.2	60.9	71.3
4	-1.0	38.7	46.8	58.9
8	-1.8	32.0	37.6	47.4
16	-2.6	24.9	30.2	36.9
32	-3.4	19.0	22.7	28.2
64	-3.1	13.2	15.8	19.7
128	-2.9	8.8	10.3	13.4
256	-2.5	6.2	7.7	10.5
512	-2.1	4.6	5.4	7.3
1,024	-1.8	3.4	4.0	5.4
2,048	-1.6	2.4	2.9	4.1
4,096	-1.6	1.7	2.0	2.7
8,192	-1.6	1.3	1.5	1.9
16,384	-1.6	0.9	1.0	1.3

Figure 11 (USAID “Extreme” poverty line): Differences and precision of differences for bootstrapped estimates of poverty rates for groups of households at a point in time, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-1.2	51.2	60.9	71.3
4	-1.2	38.8	47.1	58.3
8	-2.2	32.0	37.0	45.4
16	-2.8	24.5	28.6	35.3
32	-3.5	18.1	21.3	26.1
64	-3.6	12.3	14.9	19.7
128	-3.8	9.5	11.0	14.0
256	-3.9	6.8	8.1	10.3
512	-3.8	4.8	5.9	7.6
1,024	-3.9	3.4	4.1	5.2
2,048	-3.9	2.3	2.9	3.9
4,096	-3.9	1.8	2.1	2.7
8,192	-3.9	1.3	1.5	1.9
16,384	-4.0	0.9	1.1	1.3

Figure 13 (USAID “Extreme” poverty line): Households by targeting classification and score, along with “Total Accuracy” and BPAC, scorecard applied to the validation sample

Score	Inclusion: < poverty line correctly targeted	Undercoverage: < poverty line mistakenly non-targeted	Leakage: ? poverty line mistakenly targeted	Exclusion: ? poverty line correctly non-targeted	Total Accuracy Inclusion + Exclusion	BPAC See text
0–4	0.1	30.4	0.1	69.3	69.4	-98.6
5–9	0.4	30.2	0.2	69.2	69.6	-96.8
10–14	2.3	28.3	0.9	68.6	70.9	-82.1
15–19	5.2	25.3	1.7	67.8	73.0	-60.3
20–24	7.7	22.9	3.1	66.4	74.1	-39.8
25–29	14.0	16.5	7.3	62.1	76.1	15.8
30–34	18.6	11.9	11.0	58.5	77.1	57.7
35–39	23.9	6.6	19.1	50.3	74.2	37.3
40–44	27.4	3.2	27.1	42.3	69.7	11.2
45–49	28.5	2.1	32.1	37.3	65.8	-5.2
50–54	29.9	0.7	38.8	30.7	60.6	-26.9
55–59	30.3	0.2	47.1	22.4	52.7	-54.1
60–64	30.5	0.0	52.8	16.6	47.1	-73.0
65–69	30.5	0.0	58.2	11.3	41.8	-90.4
70–74	30.5	0.0	62.5	6.9	37.5	-104.7
75–79	30.5	0.0	65.5	4.0	34.5	-114.4
80–84	30.5	0.0	67.9	1.6	32.1	-122.2
85–89	30.5	0.0	68.7	0.7	31.3	-125.0
90–94	30.5	0.0	69.2	0.3	30.8	-126.6
95–100	30.5	0.0	69.5	0.0	30.5	-127.4

Inclusion, undercoverage, leakage, and exclusion normalized to sum to 100.

Figure 14 (USAID “Extreme” poverty line): Households below the poverty line and all households, at a given score or at or below a given score cut-off, scorecard applied to the validation sample

Score	People below poverty line (%)		All people (%)	
	At score	At or below score	At score	At or below score
0–4	49.2	49.2	0.3	0.3
5–9	79.1	64.6	0.3	0.6
10–14	74.2	72.4	2.6	3.2
15–19	79.0	76.0	3.7	6.9
20–24	63.4	71.5	3.8	10.7
25–29	59.8	65.7	10.6	21.4
30–34	55.8	62.9	8.2	29.6
35–39	39.5	55.6	13.5	43.1
40–44	30.0	50.2	11.4	54.5
45–49	18.0	47.0	6.1	60.6
50–54	17.5	43.5	8.0	68.6
55–59	5.0	39.2	8.8	77.4
60–64	3.6	36.6	6.0	83.4
65–69	0.1	34.4	5.3	88.7
70–74	0.4	32.8	4.4	93.1
75–79	0.0	31.8	3.0	96.0
80–84	0.0	31.0	2.4	98.4
85–89	0.0	30.8	0.8	99.3
90–94	0.0	30.6	0.5	99.7
95–100	0.0	30.5	0.3	100.0

\$1/Day Poverty Line Tables

Figure 4 (\$1/Day poverty line): Estimated poverty likelihoods associated with scores

If an individual's score is then the likelihood (%) of being below the poverty line is:
0–4	72.8
5–9	86.9
10–14	71.2
15–19	66.8
20–24	60.4
25–29	50.3
30–34	58.3
35–39	25.8
40–44	27.2
45–49	13.0
50–54	10.2
55–59	3.5
60–64	0.8
65–69	0.0
70–74	0.4
75–79	0.0
80–84	0.0
85–89	0.0
90–94	0.0
95–100	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 5 (\$1/Day poverty line): Derivation of estimated poverty likelihoods associated with scores

Score	People below poverty line		All people at score		Poverty likelihood (estimated, %)
0-4	208	÷	286	=	72.8
5-9	262	÷	302	=	86.9
10-14	1,837	÷	2,582	=	71.2
15-19	2,488	÷	3,725	=	66.8
20-24	2,309	÷	3,825	=	60.4
25-29	5,354	÷	10,638	=	50.3
30-34	4,782	÷	8,210	=	58.3
35-39	3,484	÷	13,527	=	25.8
40-44	3,102	÷	11,414	=	27.2
45-49	793	÷	6,093	=	13.0
50-54	819	÷	8,033	=	10.2
55-59	308	÷	8,760	=	3.5
60-64	47	÷	5,975	=	0.8
65-69	0	÷	5,327	=	0.0
70-74	18	÷	4,386	=	0.4
75-79	0	÷	2,965	=	0.0
80-84	0	÷	2,379	=	0.0
85-89	0	÷	846	=	0.0
90-94	0	÷	477	=	0.0
95-100	0	÷	251	=	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 7 (\$1/Day poverty line): Bootstrapped differences between estimated and true poverty likelihoods for households in a large sample ($n = 16,384$), with confidence intervals, scorecard applied to the validation sample

Scorecard applied to validation sample, difference between estimate and true value				
Score	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
0-4	48.3	9.0	10.7	14.6
5-9	11.4	11.7	13.5	19.0
10-14	21.5	5.7	6.5	8.5
15-19	-12.6	7.7	8.0	8.6
20-24	1.8	3.7	4.6	6.3
25-29	7.4	2.3	2.8	3.8
30-34	-20.9	11.4	11.5	11.8
35-39	6.8	1.5	1.9	2.6
40-44	-17.1	10.1	10.3	10.9
45-49	1.0	1.7	2.0	2.5
50-54	-6.1	4.0	4.2	4.6
55-59	2.2	0.3	0.4	0.5
60-64	-1.0	0.9	0.9	1.1
65-69	0.0	0.0	0.0	0.0
70-74	0.3	0.1	0.1	0.1
75-79	0.0	0.0	0.0	0.0
80-84	0.0	0.0	0.0	0.0
85-89	0.0	0.0	0.0	0.0
90-94	0.0	0.0	0.0	0.0
95-100	0.0	0.0	0.0	0.0

Figure 9 (\$1/Day poverty line): Differences and precision of differences for bootstrapped estimates of households' poverty likelihoods, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-1.0	50.4	59.7	68.9
4	-0.5	37.0	47.5	57.0
8	-1.6	32.8	38.2	48.2
16	-2.7	25.5	30.7	36.0
32	-3.8	19.4	21.9	28.3
64	-3.6	13.4	15.7	19.6
128	-3.4	9.0	10.5	14.2
256	-3.0	6.3	7.8	10.7
512	-2.5	4.7	5.6	7.6
1,024	-2.2	3.5	4.1	5.2
2,048	-2.1	2.4	2.9	4.1
4,096	-2.0	1.7	2.0	2.7
8,192	-2.1	1.3	1.5	2.0
16,384	-2.1	0.9	1.0	1.3

Figure 11 (\$1/Day poverty line): Differences and precision of differences for bootstrapped estimates of poverty rates for groups of households at a point in time, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-1.0	50.4	59.7	68.9
4	-0.7	37.5	47.7	56.6
8	-1.7	32.0	37.2	46.1
16	-2.6	25.4	28.7	35.4
32	-3.5	18.3	21.4	27.0
64	-3.6	13.0	15.2	20.1
128	-3.9	9.6	11.4	14.1
256	-4.0	7.0	8.5	10.7
512	-4.0	4.9	5.9	7.7
1,024	-4.0	3.5	4.1	5.4
2,048	-4.0	2.4	2.9	4.2
4,096	-4.0	1.8	2.1	2.7
8,192	-4.1	1.3	1.6	1.9
16,384	-4.1	0.9	1.1	1.4

Figure 13 (\$1/Day poverty line): Households by targeting classification and score, along with “Total Accuracy” and BPAC, scorecard applied to the validation sample

Score	Inclusion: < poverty line correctly targeted	Undercoverage: < poverty line mistakenly non-targeted	Leakage: ? poverty line mistakenly targeted	Exclusion: ? poverty line correctly non-targeted	Total Accuracy Inclusion + Exclusion	BPAC See text
0-4	0.1	27.0	0.1	72.8	72.9	-98.4
5-9	0.4	26.7	0.2	72.7	73.1	-96.4
10-14	2.2	24.9	0.9	72.0	74.2	-80.0
15-19	5.0	22.1	1.8	71.1	76.1	-55.9
20-24	7.1	20.0	3.6	69.3	76.5	-34.1
25-29	12.5	14.6	8.9	64.0	76.5	24.9
30-34	17.0	10.1	12.6	60.3	77.3	53.6
35-39	21.7	5.4	21.4	51.5	73.2	21.1
40-44	24.3	2.8	30.2	42.7	67.0	-11.4
45-49	25.3	1.8	35.3	37.6	63.0	-30.2
50-54	26.6	0.5	42.1	30.8	57.4	-55.2
55-59	26.9	0.2	50.5	22.4	49.3	-86.3
60-64	27.1	0.0	56.3	16.6	43.7	-107.7
65-69	27.1	0.0	61.6	11.3	38.4	-127.4
70-74	27.1	0.0	66.0	6.9	34.0	-143.5
75-79	27.1	0.0	68.9	4.0	31.1	-154.4
80-84	27.1	0.0	71.3	1.6	28.7	-163.2
85-89	27.1	0.0	72.2	0.7	27.8	-166.3
90-94	27.1	0.0	72.7	0.3	27.3	-168.1
95-100	27.1	0.0	72.9	0.0	27.1	-169.0

Inclusion, undercoverage, leakage, and exclusion normalized to sum to 100.

Figure 14 (\$1/Day poverty line): Households below the poverty line and all households, at a given score or at or below a given score cut-off, scorecard applied to the validation sample

Score	People below poverty line (%)		All people (%)	
	At score	At or below score	At score	At or below score
0-4	49.2	49.2	0.3	0.3
5-9	79.1	64.6	0.3	0.6
10-14	71.9	70.6	2.6	3.2
15-19	75.4	73.2	3.7	6.9
20-24	54.9	66.7	3.8	10.7
25-29	50.1	58.4	10.6	21.4
30-34	54.9	57.4	8.2	29.6
35-39	34.9	50.4	13.5	43.1
40-44	22.9	44.6	11.4	54.5
45-49	16.5	41.8	6.1	60.6
50-54	15.5	38.7	8.0	68.6
55-59	3.8	34.8	8.8	77.4
60-64	2.9	32.5	6.0	83.4
65-69	0.1	30.5	5.3	88.7
70-74	0.4	29.1	4.4	93.1
75-79	0.0	28.2	3.0	96.0
80-84	0.0	27.5	2.4	98.4
85-89	0.0	27.3	0.8	99.3
90-94	0.0	27.2	0.5	99.7
95-100	0.0	27.1	0.3	100.0

\$2/Day Poverty Line Tables

Figure 4 (\$2/Day poverty line): Estimated poverty likelihoods associated with scores

If an individual's score is then the likelihood (%) of being below the poverty line is:
0–4	100.0
5–9	86.9
10–14	99.5
15–19	96.7
20–24	94.5
25–29	92.6
30–34	90.5
35–39	83.6
40–44	85.4
45–49	70.5
50–54	57.3
55–59	30.4
60–64	26.0
65–69	7.4
70–74	8.3
75–79	7.8
80–84	0.8
85–89	0.0
90–94	5.9
95–100	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 5 (\$2/Day poverty line): Derivation of estimated poverty likelihoods associated with scores

Score	People below poverty line		All people at score		Poverty likelihood (estimated, %)
0–4	286	÷	286	=	100.0
5–9	262	÷	302	=	86.9
10–14	2,568	÷	2,582	=	99.5
15–19	3,601	÷	3,725	=	96.7
20–24	3,614	÷	3,825	=	94.5
25–29	9,853	÷	10,638	=	92.6
30–34	7,431	÷	8,210	=	90.5
35–39	11,307	÷	13,527	=	83.6
40–44	9,751	÷	11,414	=	85.4
45–49	4,293	÷	6,093	=	70.5
50–54	4,606	÷	8,033	=	57.3
55–59	2,660	÷	8,760	=	30.4
60–64	1,553	÷	5,975	=	26.0
65–69	392	÷	5,327	=	7.4
70–74	365	÷	4,386	=	8.3
75–79	232	÷	2,965	=	7.8
80–84	19	÷	2,379	=	0.8
85–89	0	÷	846	=	0.0
90–94	28	÷	477	=	5.9
95–100	0	÷	251	=	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 7 (\$2/Day poverty line): Bootstrapped differences between estimated and true poverty likelihoods for households in a large sample ($n = 16,384$), with confidence intervals, scorecard applied to the validation sample

Scorecard applied to validation sample, difference between estimate and true value				
Score	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
0-4	0.0	0.0	0.0	0.0
5-9	-13.1	6.6	6.6	6.6
10-14	-0.2	0.2	0.3	0.4
15-19	-2.5	1.4	1.5	1.5
20-24	8.7	3.3	3.9	4.9
25-29	3.8	1.4	1.7	2.2
30-34	-6.6	3.5	3.6	3.7
35-39	-5.6	3.4	3.5	3.8
40-44	-7.3	4.1	4.1	4.2
45-49	9.6	3.3	3.8	5.1
50-54	2.0	2.4	3.0	4.1
55-59	14.5	1.7	2.0	2.7
60-64	-12.5	7.8	8.1	8.8
65-69	-1.8	1.7	1.9	2.3
70-74	1.6	1.5	1.9	2.4
75-79	0.2	1.9	2.2	2.9
80-84	0.7	0.1	0.1	0.1
85-89	-37.3	23.3	24.0	25.2
90-94	5.9	0.0	0.0	0.0
95-100	0.0	0.0	0.0	0.0

Figure 9 (\$2/Day poverty line): Differences and precision of differences for bootstrapped estimates of households' poverty likelihoods, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-0.5	49.2	59.1	73.1
4	-0.3	34.5	41.8	56.7
8	-0.9	23.2	29.7	41.8
16	-1.0	17.0	20.9	27.4
32	-0.5	12.8	15.5	20.2
64	-0.2	8.7	10.6	13.3
128	-0.2	5.9	7.2	9.5
256	-0.4	4.5	5.3	6.6
512	-0.6	3.2	3.9	5.0
1,024	-0.6	2.2	2.5	3.3
2,048	-0.7	1.5	1.9	2.3
4,096	-0.6	1.1	1.3	1.8
8,192	-0.6	0.7	0.9	1.3
16,384	-0.6	0.6	0.7	0.8

Figure 11 (\$2/Day poverty line): Differences and precision of differences for bootstrapped estimates of poverty rates for groups of households at a point in time, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	-0.5	49.2	59.1	73.1
4	-0.4	33.2	40.2	57.9
8	-0.8	22.9	28.9	40.2
16	-0.9	16.5	19.6	25.0
32	-0.7	11.9	14.0	19.5
64	-0.6	8.4	10.1	13.1
128	-0.6	5.8	7.1	9.8
256	-0.7	4.3	5.2	6.9
512	-0.7	3.2	3.9	5.0
1,024	-0.7	2.1	2.5	3.6
2,048	-0.7	1.6	1.8	2.3
4,096	-0.7	1.1	1.3	1.7
8,192	-0.7	0.8	0.9	1.3
16,384	-0.7	0.5	0.6	0.9

Figure 13 (\$2/Day poverty line): Households by targeting classification and score, along with “Total Accuracy” and BPAC, scorecard applied to the validation sample

Score	Inclusion: < poverty line correctly targeted	Undercoverage: < poverty line mistakenly non-targeted	Leakage: ? poverty line mistakenly targeted	Exclusion: ? poverty line correctly non-targeted	Total Accuracy Inclusion + Exclusion	BPAC See text
0-4	0.3	62.9	0.0	36.8	37.1	-99.1
5-9	0.6	62.6	0.0	36.8	37.4	-98.1
10-14	3.1	60.0	0.0	36.8	39.9	-90.0
15-19	6.8	56.4	0.1	36.7	43.5	-78.3
20-24	10.3	52.9	0.4	36.4	46.7	-66.7
25-29	19.9	43.3	1.5	35.3	55.2	-34.8
30-34	27.4	35.8	2.1	34.7	62.1	-9.8
35-39	38.8	24.4	4.3	32.5	71.3	29.6
40-44	48.0	15.2	6.5	30.3	78.3	62.2
45-49	51.9	11.3	8.7	28.1	80.0	78.0
50-54	56.4	6.8	12.2	24.6	81.0	80.7
55-59	59.4	3.8	18.0	18.8	78.2	71.5
60-64	61.6	1.5	21.7	15.1	76.7	65.6
65-69	62.3	0.8	26.3	10.5	72.8	58.3
70-74	62.7	0.5	30.4	6.4	69.2	51.9
75-79	63.0	0.2	33.0	3.8	66.8	47.7
80-84	63.0	0.1	35.4	1.4	64.5	44.0
85-89	63.2	0.0	36.1	0.7	63.9	42.9
90-94	63.2	0.0	36.6	0.3	63.4	42.1
95-100	63.2	0.0	36.8	0.0	63.2	41.7

Inclusion, undercoverage, leakage, and exclusion normalized to sum to 100.

Figure 14 (\$2/Day poverty line): Households below the poverty line and all households, at a given score or at or below a given score cut-off, scorecard applied to the validation sample

Score	People below poverty line (%)		All people (%)	
	At score	At or below score	At score	At or below score
0-4	100.0	100.0	0.3	0.3
5-9	100.0	100.0	0.3	0.6
10-14	98.9	99.1	2.6	3.2
15-19	97.9	98.5	3.7	6.9
20-24	92.2	96.2	3.8	10.7
25-29	89.7	93.0	10.6	21.4
30-34	92.2	92.8	8.2	29.6
35-39	84.0	90.0	13.5	43.1
40-44	80.6	88.1	11.4	54.5
45-49	63.9	85.6	6.1	60.6
50-54	56.4	82.2	8.0	68.6
55-59	34.1	76.8	8.8	77.4
60-64	37.3	73.9	6.0	83.4
65-69	13.2	70.3	5.3	88.7
70-74	8.3	67.4	4.4	93.1
75-79	10.6	65.6	3.0	96.0
80-84	0.6	64.1	2.4	98.4
85-89	17.2	63.7	0.8	99.3
90-94	0.0	63.3	0.5	99.7
95-100	0.0	63.2	0.3	100.0

\$3/Day Poverty Line Tables

Figure 4 (\$3/Day poverty line): Estimated poverty likelihoods associated with scores

If an individual's score is then the likelihood (%) of being below the poverty line is:
0–4	100.0
5–9	100.0
10–14	100.0
15–19	100.0
20–24	99.6
25–29	97.9
30–34	98.5
35–39	90.6
40–44	95.9
45–49	91.5
50–54	88.7
55–59	68.7
60–64	55.1
65–69	59.1
70–74	42.0
75–79	26.4
80–84	38.2
85–89	39.0
90–94	10.0
95–100	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 5 (\$3/Day poverty line): Derivation of estimated poverty likelihoods associated with scores

Score	People below poverty line		All people at score		Poverty likelihood (estimated, %)
0-4	286	÷	286	=	100.0
5-9	302	÷	302	=	100.0
10-14	2,582	÷	2,582	=	100.0
15-19	3,725	÷	3,725	=	100.0
20-24	3,808	÷	3,825	=	99.6
25-29	10,411	÷	10,638	=	97.9
30-34	8,084	÷	8,210	=	98.5
35-39	12,259	÷	13,527	=	90.6
40-44	10,943	÷	11,414	=	95.9
45-49	5,573	÷	6,093	=	91.5
50-54	7,126	÷	8,033	=	88.7
55-59	6,019	÷	8,760	=	68.7
60-64	3,290	÷	5,975	=	55.1
65-69	3,147	÷	5,327	=	59.1
70-74	1,842	÷	4,386	=	42.0
75-79	783	÷	2,965	=	26.4
80-84	909	÷	2,379	=	38.2
85-89	329	÷	846	=	39.0
90-94	48	÷	477	=	10.0
95-100	0	÷	251	=	0.0

Surveyed cases weighted to represent Mali's households.

Based on the 2001 EMEP.

Figure 7 (\$3/Day poverty line): Bootstrapped differences between estimated and true poverty likelihoods for households in a large sample ($n = 16,384$), with confidence intervals, scorecard applied to the validation sample

Scorecard applied to validation sample, difference between estimate and true value				
Score	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
0-4	0.0	0.0	0.0	0.0
5-9	0.0	0.0	0.0	0.0
10-14	0.0	0.0	0.0	0.0
15-19	0.5	0.3	0.4	0.5
20-24	0.4	0.4	0.5	0.7
25-29	-0.2	0.6	0.7	0.9
30-34	0.1	0.4	0.5	0.7
35-39	-4.9	2.8	2.9	3.1
40-44	-1.0	0.8	0.8	0.9
45-49	0.5	1.6	1.9	2.6
50-54	-0.2	1.5	1.8	2.3
55-59	41.0	2.3	2.9	3.7
60-64	-9.1	6.2	6.4	7.0
65-69	18.4	3.2	3.8	5.1
70-74	5.0	3.6	4.5	5.8
75-79	-1.8	4.1	5.0	6.9
80-84	-11.7	8.3	8.7	9.7
85-89	-4.6	9.0	10.6	13.6
90-94	-25.9	18.1	18.6	20.4
95-100	-29.7	21.3	22.6	25.5

Figure 9 (\$3/Day poverty line): Differences and precision of differences for bootstrapped estimates of households' poverty likelihoods, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	1.6	44.5	53.2	68.1
4	2.2	35.9	44.4	53.4
8	3.2	29.8	35.1	41.6
16	4.2	22.1	26.3	35.3
32	5.4	18.1	21.1	26.4
64	6.0	12.9	15.2	20.1
128	5.9	9.4	10.8	13.2
256	5.4	6.6	7.6	10.2
512	5.2	4.6	5.7	7.5
1,024	5.0	3.3	3.8	4.8
2,048	5.0	2.4	2.7	3.8
4,096	5.1	1.6	1.9	2.6
8,192	5.1	1.1	1.3	1.7
16,384	5.1	0.7	0.9	1.2

Figure 11 (\$3/Day poverty line): Differences and precision of differences for bootstrapped estimates of poverty rates for groups of households at a point in time, by sample size, scorecard applied to the validation sample

Sample size (n)	Difference between estimate and true value			
	Diff.	Confidence interval (+/- percentage points)		
		90-percent	95-percent	99-percent
2	1.6	44.5	53.2	68.1
4	2.2	35.5	44.0	53.6
8	3.0	28.6	33.9	41.4
16	3.9	20.6	24.5	32.2
32	4.6	15.6	18.7	23.1
64	5.0	11.4	13.5	17.0
128	5.1	8.5	10.1	12.8
256	4.9	5.9	7.2	9.9
512	5.0	4.2	5.0	7.0
1,024	5.0	3.0	3.4	4.5
2,048	5.0	2.1	2.6	3.3
4,096	5.0	1.5	1.8	2.2
8,192	5.0	1.1	1.3	1.6
16,384	5.0	0.7	0.9	1.1

Figure 13 (\$3/Day poverty line): Households by targeting classification and score, along with “Total Accuracy” and BPAC, scorecard applied to the validation sample

Score	Inclusion: < poverty line correctly targeted	Undercoverage: < poverty line mistakenly non-targeted	Leakage: ? poverty line mistakenly targeted	Exclusion: ? poverty line correctly non-targeted	Total Accuracy Inclusion + Exclusion	BPAC See text
0–4	0.3	79.7	0.0	20.0	20.3	-99.3
5–9	0.6	79.4	0.0	20.0	20.6	-98.5
10–14	3.2	76.9	0.0	20.0	23.1	-92.1
15–19	6.9	73.2	0.0	19.9	26.8	-82.8
20–24	10.6	69.4	0.1	19.9	30.5	-73.3
25–29	21.1	58.9	0.3	19.7	40.8	-47.0
30–34	29.0	51.1	0.6	19.4	48.4	-26.8
35–39	41.7	38.3	1.4	18.6	60.4	6.0
40–44	52.3	27.7	2.2	17.7	70.0	33.4
45–49	57.6	22.4	3.0	17.0	74.6	47.7
50–54	64.6	15.5	4.1	15.9	80.5	66.5
55–59	69.9	10.1	7.5	12.5	82.4	84.0
60–64	73.8	6.2	9.5	10.4	84.3	88.1
65–69	76.2	3.9	12.5	7.4	83.6	84.3
70–74	77.8	2.2	15.2	4.7	82.6	80.9
75–79	78.7	1.3	17.3	2.7	81.4	78.4
80–84	79.6	0.4	18.8	1.2	80.8	76.5
85–89	79.8	0.2	19.4	0.5	80.4	75.7
90–94	80.0	0.1	19.8	0.2	80.2	75.3
95–100	80.0	0.0	20.0	0.0	80.0	75.0

Inclusion, undercoverage, leakage, and exclusion normalized to sum to 100.

Figure 14 (\$3/Day poverty line): Households below the poverty line and all households, at a given score or at or below a given score cut-off, scorecard applied to the validation sample

Score	People below poverty line (%)		All people (%)	
	At score	At or below score	At score	At or below score
0-4	100.0	100.0	0.3	0.3
5-9	100.0	100.0	0.3	0.6
10-14	100.0	100.0	2.6	3.2
15-19	98.9	99.4	3.7	6.9
20-24	98.5	99.1	3.8	10.7
25-29	98.3	98.7	10.6	21.4
30-34	96.1	98.0	8.2	29.6
35-39	94.3	96.9	13.5	43.1
40-44	92.3	95.9	11.4	54.5
45-49	88.0	95.1	6.1	60.6
50-54	86.3	94.1	8.0	68.6
55-59	60.7	90.3	8.8	77.4
60-64	66.2	88.6	6.0	83.4
65-69	43.6	85.9	5.3	88.7
70-74	38.0	83.6	4.4	93.1
75-79	30.4	82.0	3.0	96.0
80-84	36.8	80.9	2.4	98.4
85-89	27.0	80.4	0.8	99.3
90-94	26.8	80.2	0.5	99.7
95-100	22.8	80.0	0.3	100.0